

# NMR in Medicine and Biology

[http://en.wikipedia.org/wiki/NMR\\_Spectroscopy](http://en.wikipedia.org/wiki/NMR_Spectroscopy)

- **MRI- Magnetic Resonance Imaging (water)**
- **In-vivo spectroscopy (metabolites)**
- **Solid-state NMR (large structures)**
- **Solution NMR Spectroscopy**
  - Analytical biochemistry
  - Comparative analysis
  - Interactions between biomolecules
  - Ligand screening (SAR by NMR)
  - Structure determination
  - Protein Dynamics

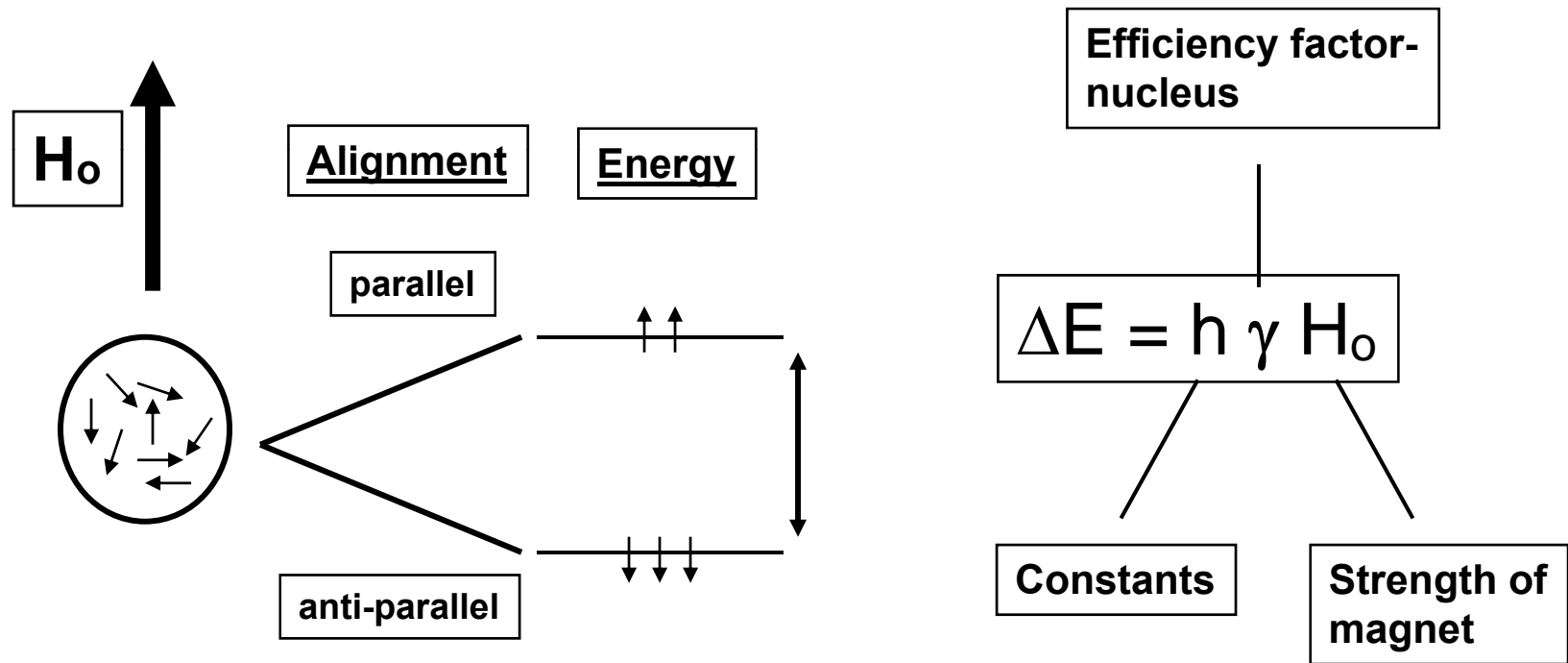
# *Protein NMR*

## *Detection of spin 1/2 nuclei*

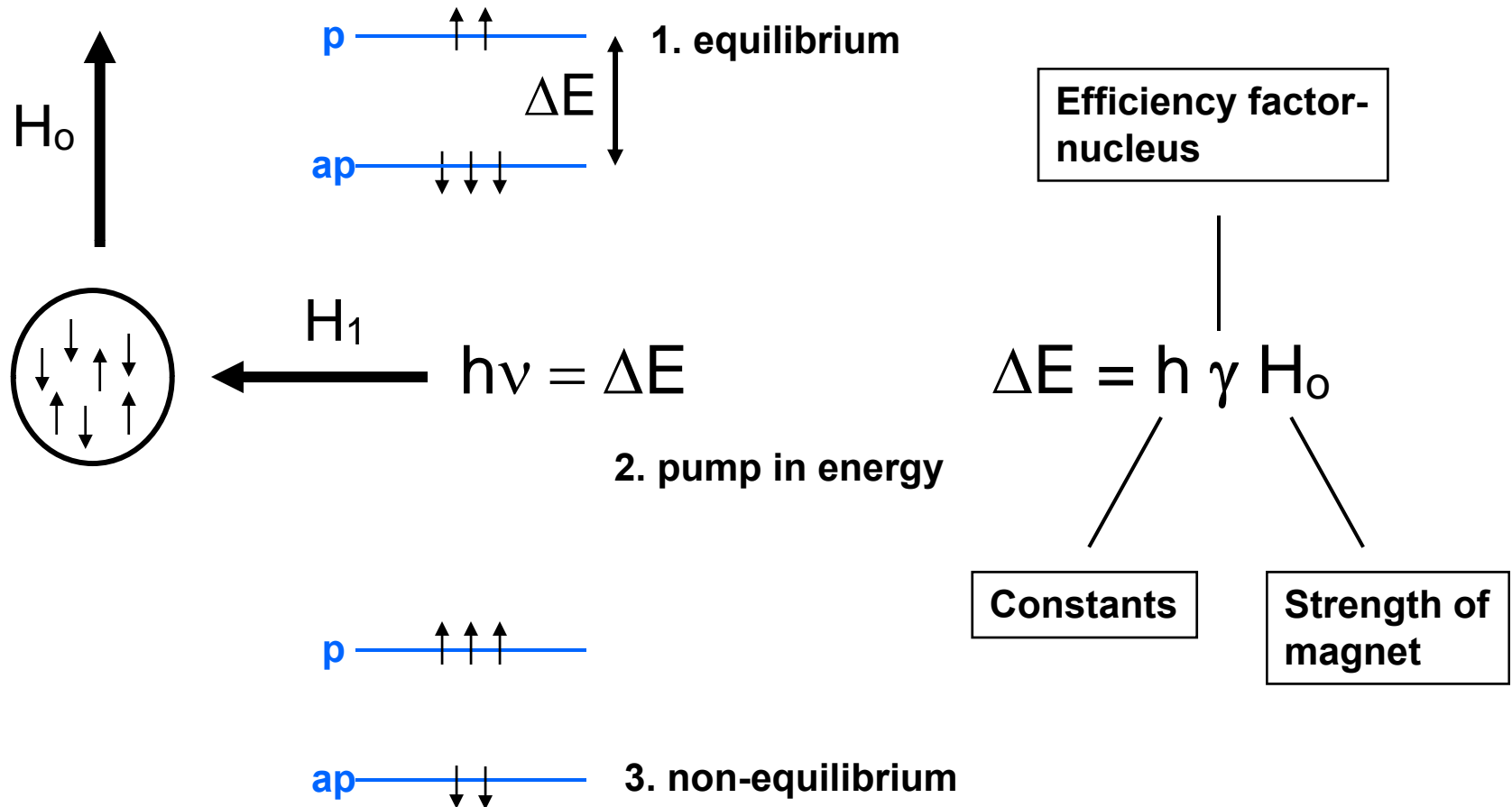
### $^1\text{H}$ , $^{13}\text{C}$ , $^{15}\text{N}$ , $^{31}\text{P}$

- Only nuclei with *spin number* ( $I$ )  $\neq 0$  can absorb/emit electromagnetic radiation.
  - Even atomic mass & number  $\Rightarrow I = 0$  ( $^{12}\text{C}$ ,  $^{16}\text{O}$ )
  - Even atomic mass & odd number  $\Rightarrow I = \text{whole integer}$  ( $^{14}\text{N}$ ,  $^2\text{H}$ ,  $^{10}\text{B}$ )
  - Odd atomic mass  $\Rightarrow I = \text{half integer}$  ( $^1\text{H}$ ,  $^{13}\text{C}$ ,  $^{15}\text{N}$ ,  $^{31}\text{P}$ )
- Nuclear spin angular momentum is a quantized property of the nucleus in each atom

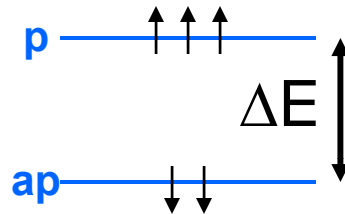
# Nuclei With Non-Zero Spin Align in Magnetic Fields



# Resonance: Perturb Equilibrium



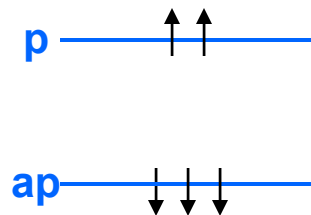
# Return to Equilibrium (Relax): Read Out Signals



3. Non-equilibrium

$$h\nu = \Delta E$$

4. release energy (detect)



5. equilibrium

# Magnetic Resonance Sensitivity

Sensitivity (S) ~  $\Delta(\text{population})$

$$S \sim \Delta N = \frac{N_p}{N_{ap}} = e^{-\Delta E/kT}$$

Efficiency factor-nucleus

$$\Delta E = h \gamma H_0$$

Constants

Strength of magnet

$\Delta E$  is small

At room temp.,  $\Delta N \sim 1:10^5$

**Intrinsically low sensitivity** →

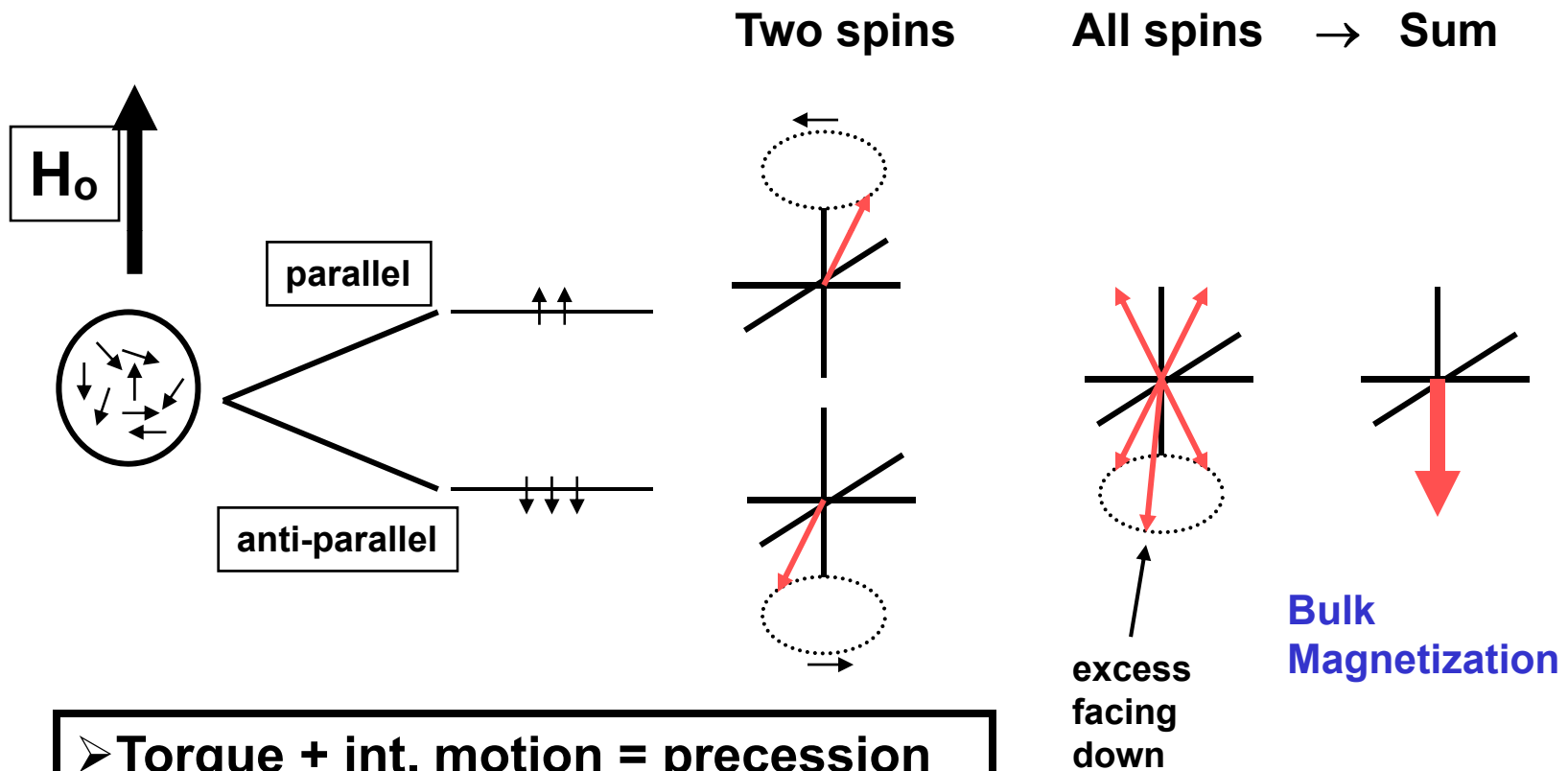
**Need lots of sample**

*Increase sensitivity by increasing magnetic field strength  
And high protein concentration*

# Intrinsic Sensitivity of Nuclei

<b>Nucleus</b>	<b><math>\gamma</math></b>	<b>% Natural Abundance</b>	<b>Relative Sensitivity</b>
<b><math>^1\text{H}</math></b>	<b><math>2.7 \times 10^8</math></b>	<b>99.98</b>	<b>1.0</b>
<b><math>^{13}\text{C}</math></b>	<b><math>6.7 \times 10^7</math></b>	<b>1.11</b>	<b>0.004</b>
<b><math>^{15}\text{N}</math></b>	<b><math>-2.7 \times 10^7</math></b>	<b>0.36</b>	<b>0.0004</b>
<b><math>^{31}\text{P}</math></b>	<b><math>1.1 \times 10^8</math></b>	<b>100.</b>	<b>0.5</b>

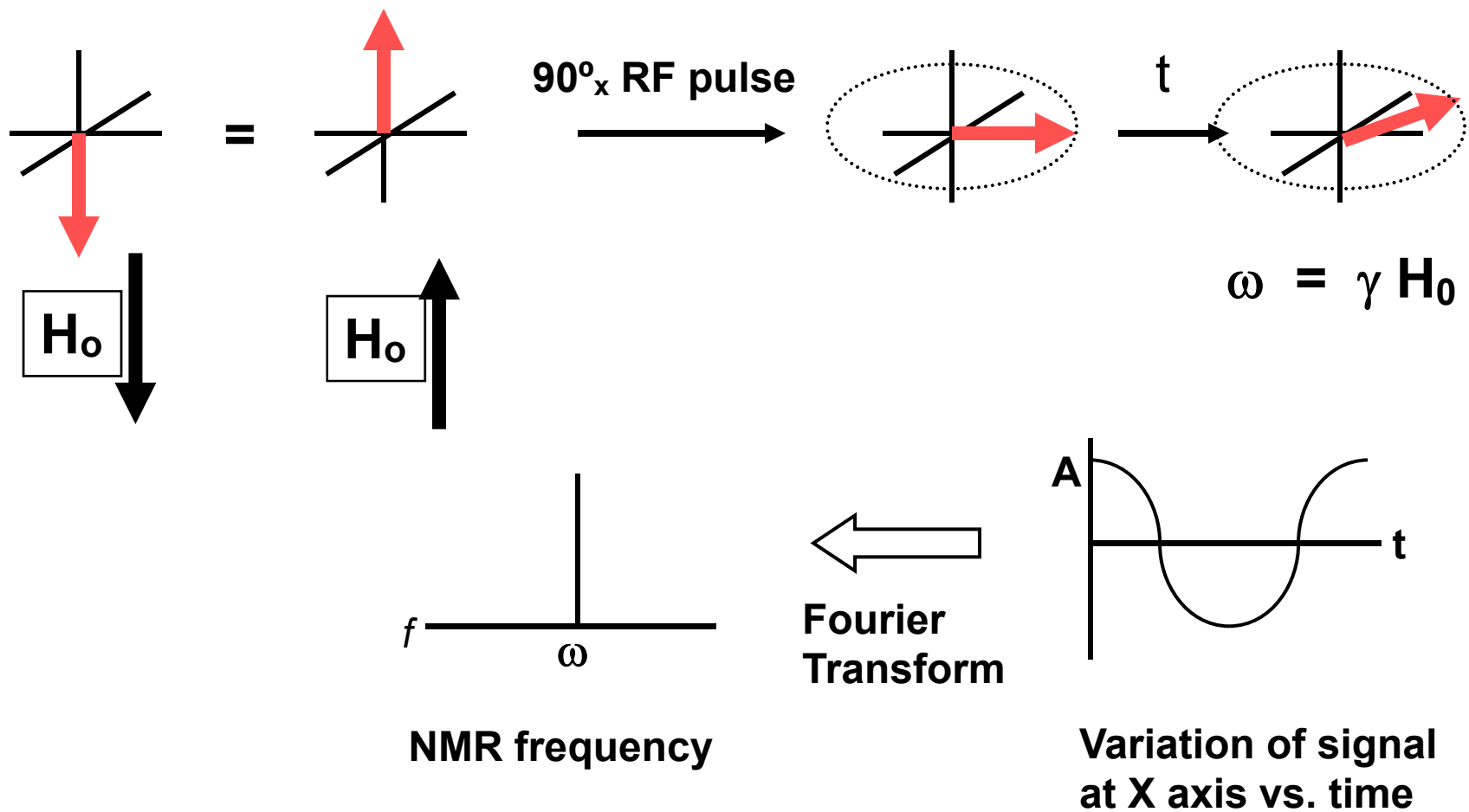
# The Classical Treatment: Nuclear Spin Angular Momentum



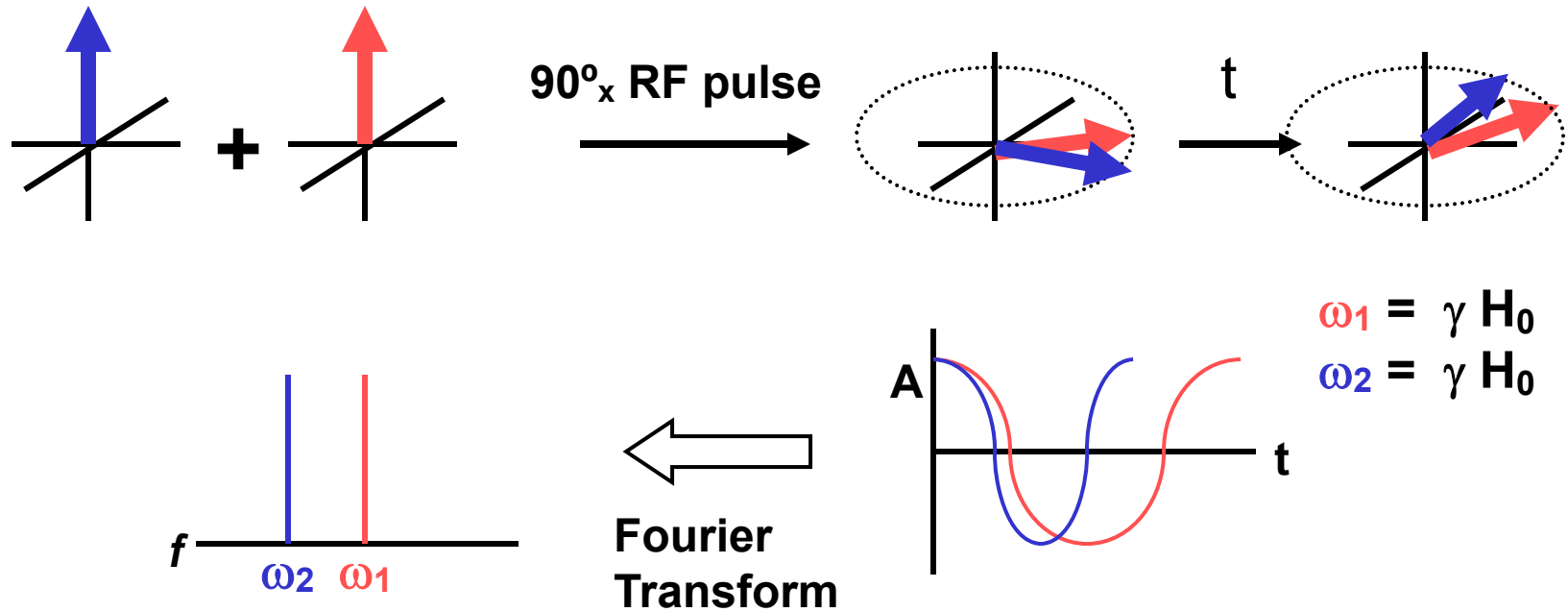
- Torque + int. motion = precession
- Precession around Z axis
- Larmor frequency ( $\omega$ ):  

$$\Delta E = h\gamma H_0 \rightarrow \Delta E = h\nu \rightarrow \nu = \gamma H_0 = \omega$$

# Pulse Fourier Transform NMR



# The Power of Fourier Transform

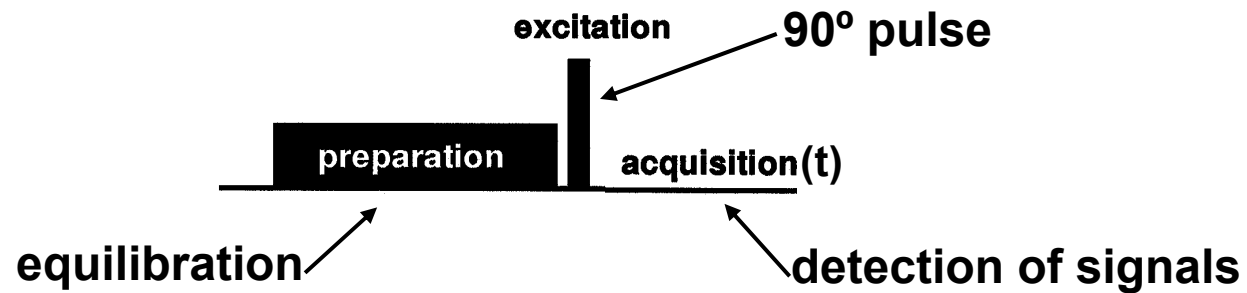


**NMR frequency domain**  
➤ Spectrum of frequencies

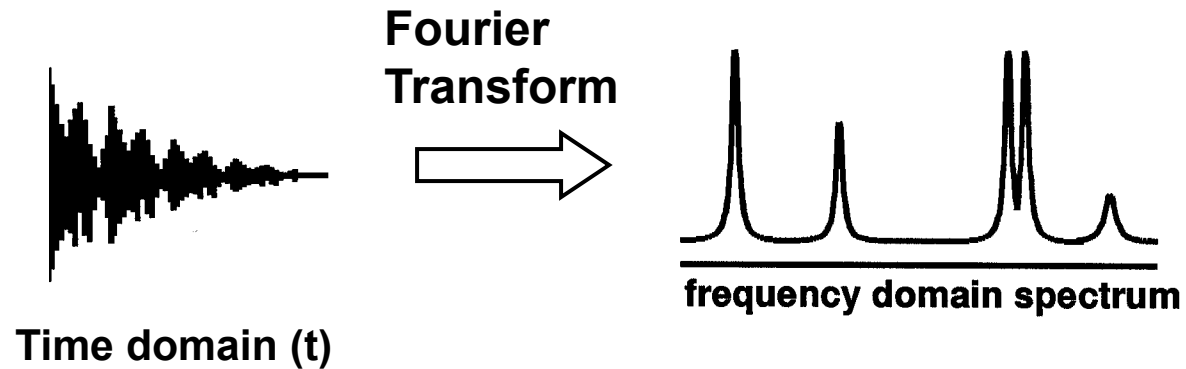
**NMR time domain**  
➤ Variation in amplitude vs time

# The Pulse FT NMR Experiment

## Experiment



## Data Analysis



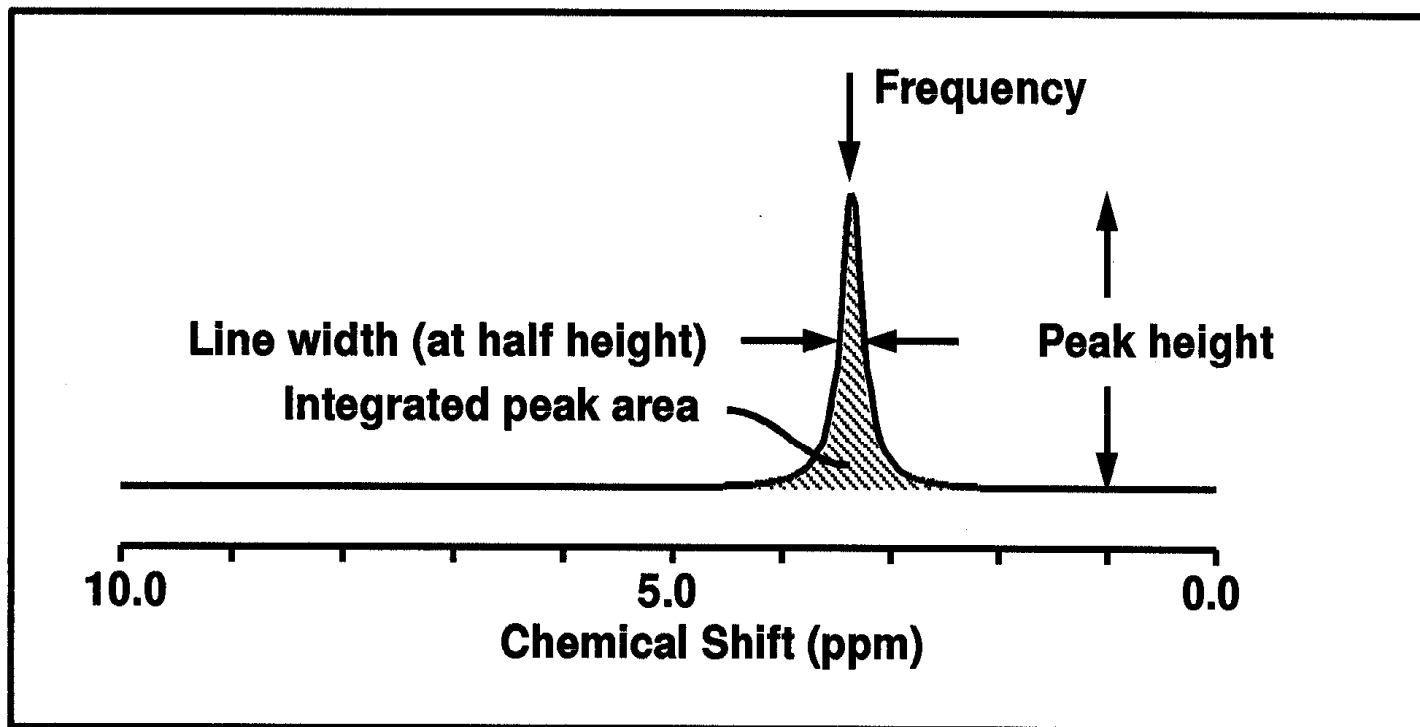
# NMR Terminology

$$\delta = \frac{\omega - \omega_{\text{ref}}}{\omega_{\text{ref}}}$$

ppm (parts per million), Universal Unit

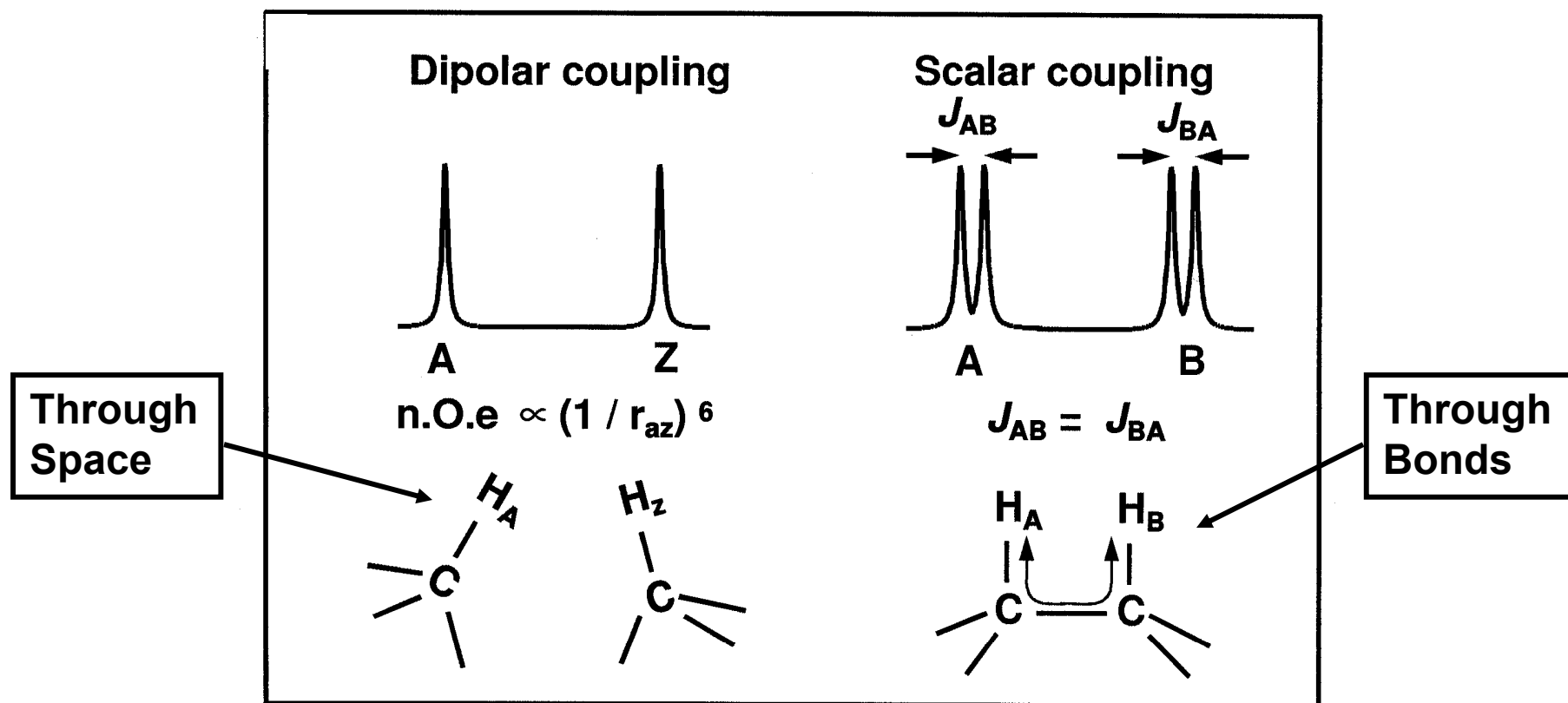
Universal Reference

1. Samples in water
2. Organic compounds



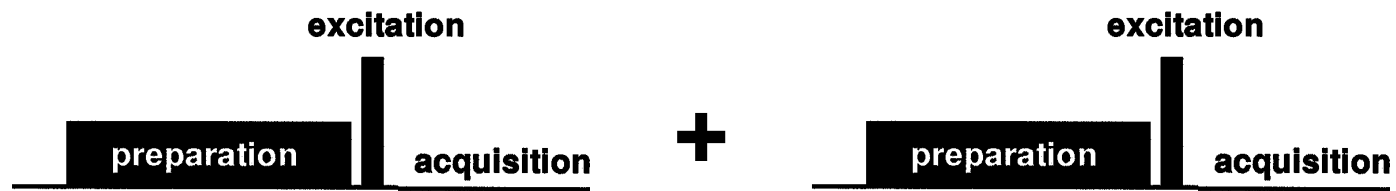
*The exact resonance frequency (chemical shift) is determined by the electronic environment of the nucleus*

# NMR Scalar and Dipolar Coupling

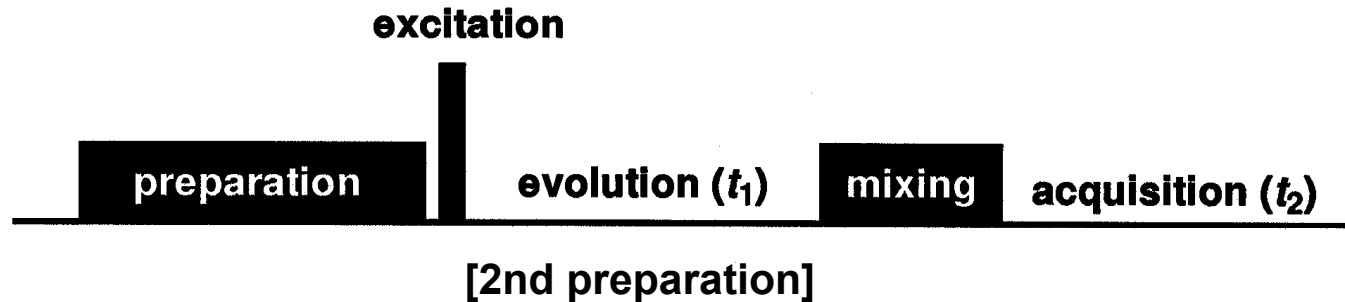


➤ **Coupling of nuclei gives information on structure**

# The 2D NMR Pulse Sequence

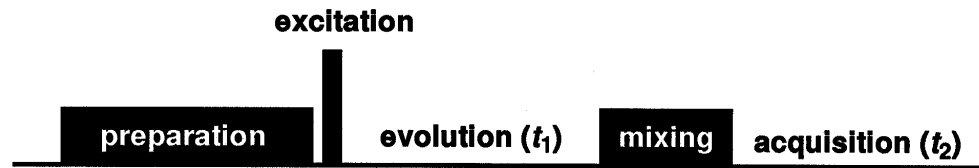


$$1D + 1D = 2D$$



# The 2D NMR Spectrum

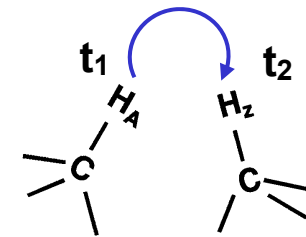
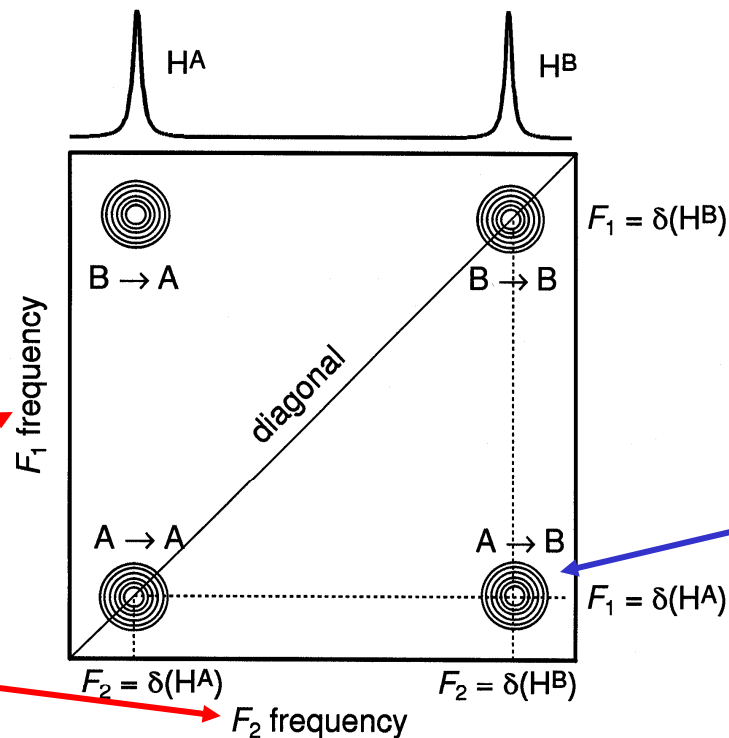
Pulse Sequence



Spectrum

Before mixing

After mixing



Coupled spins  
give rise to  
crosspeaks

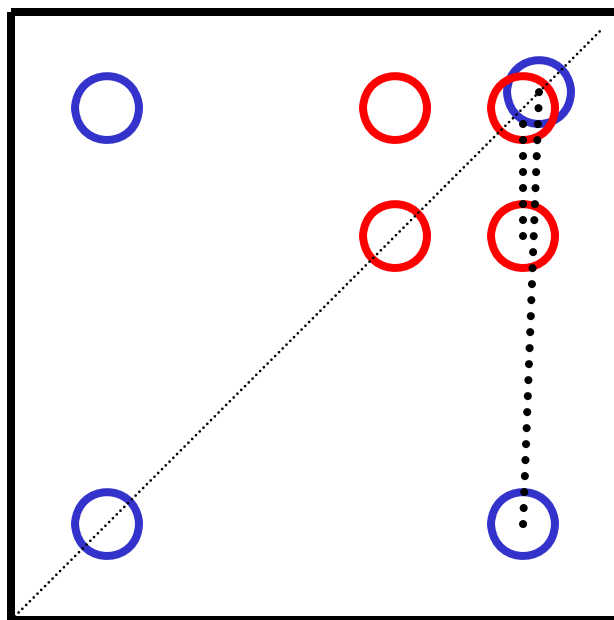
# The Power of 2D NMR: Resolving Overlapping Signals

1D



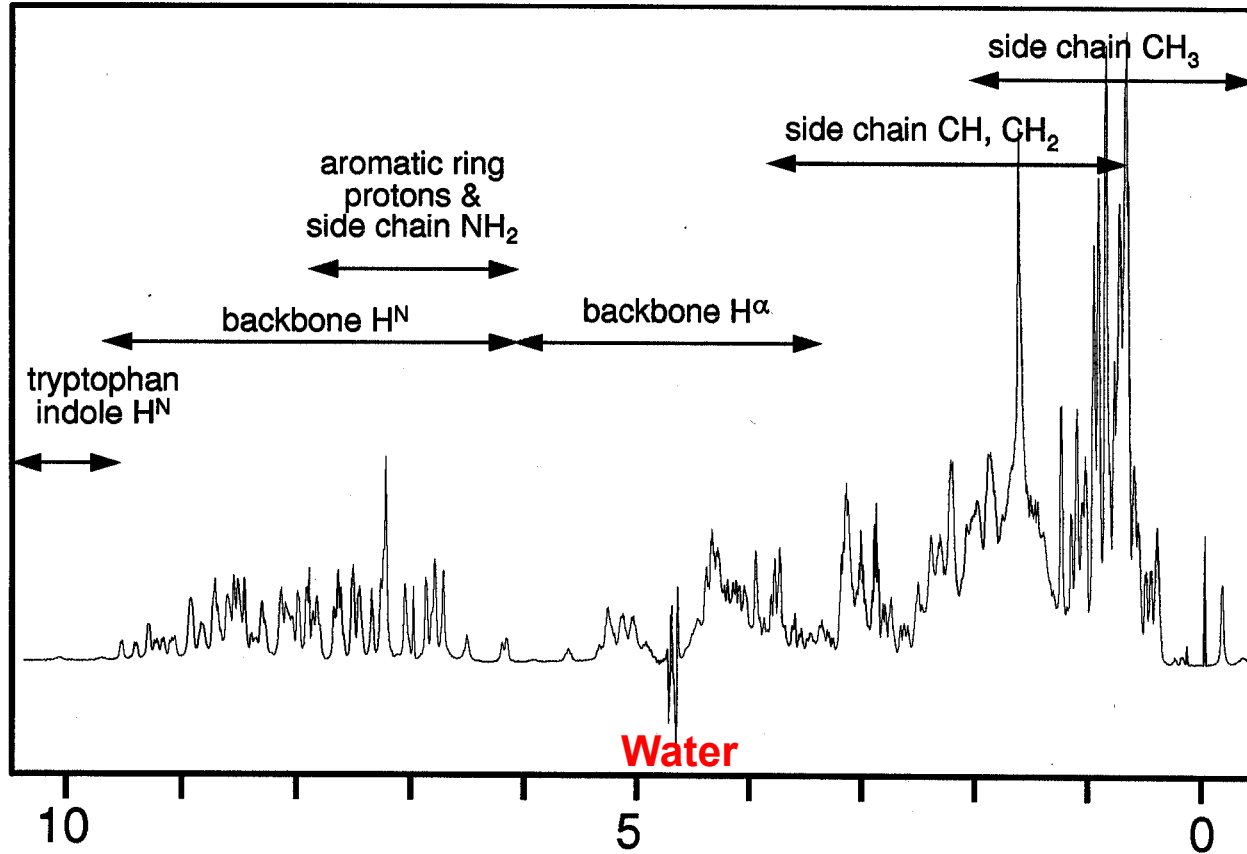
2 signals  
overlapped

2D



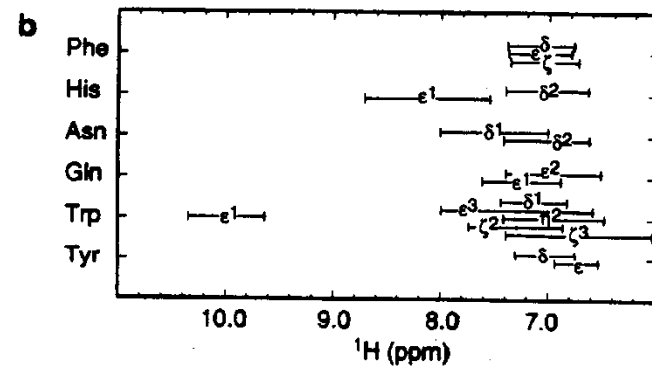
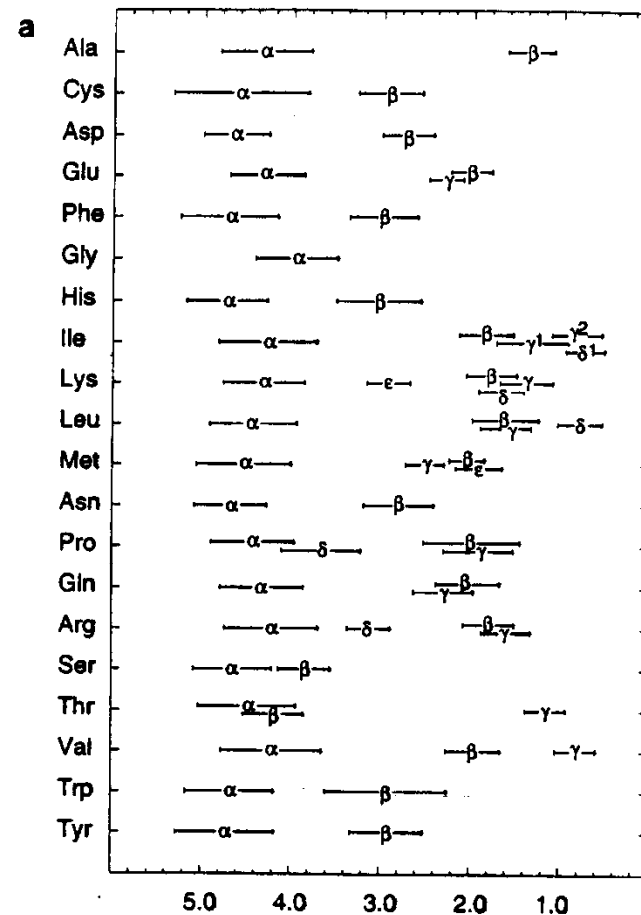
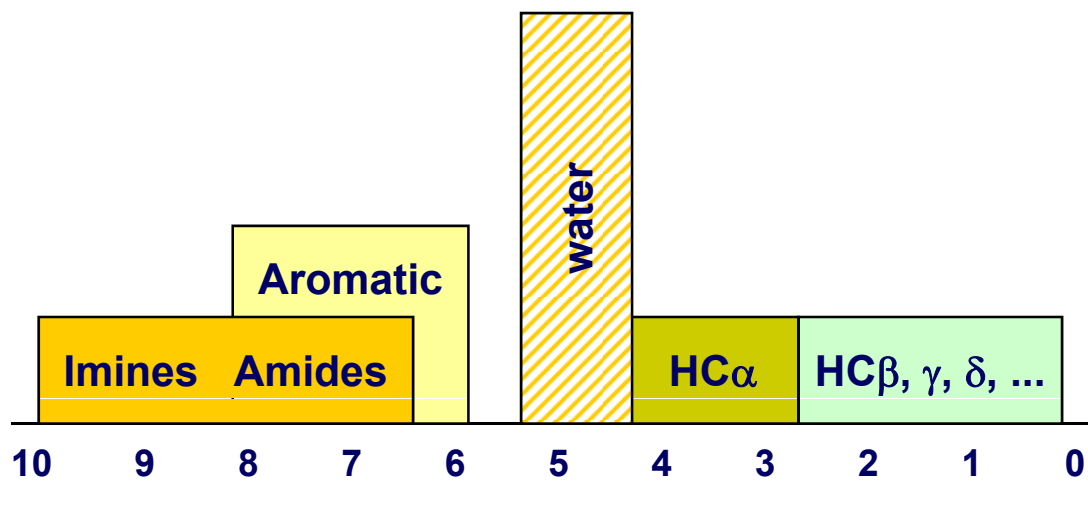
2 cross peaks  
resolved

# Regions of the $^1\text{H}$ NMR Spectrum



What would the unfolded protein look like?

Each side chain proton has characteristic ppm range of signal on the NMR spectrum.



# **NMR of Proteins**

## **Challenges**

**Proteins have hundreds/thousands of signals**

**Resonance assignment first (who do all these signals belong to?)**

**Computer programs can be used to get assistance with resonance assignments**

## **Applications**

**Folded protein?**

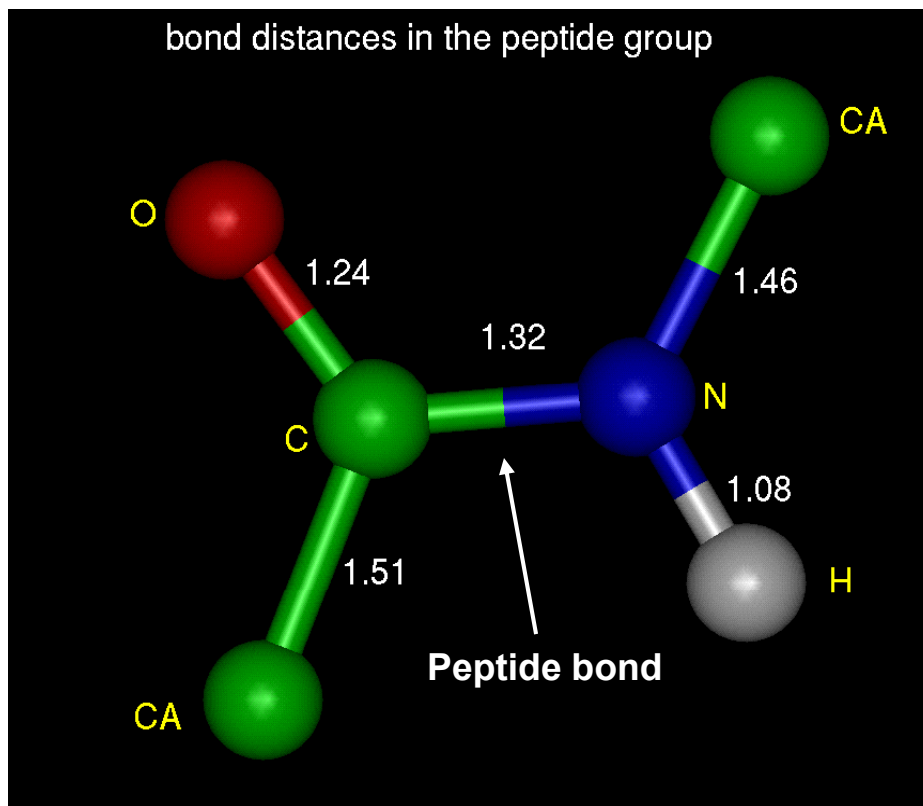
**Measure binding constants**

**Assess structural homology/effect of mutations**

**Three-dimensional structure determination**

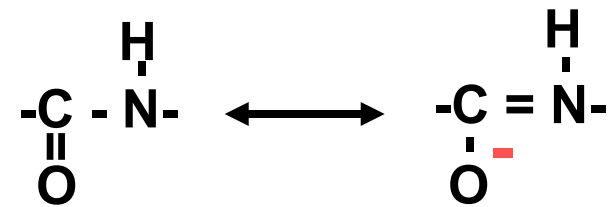
**Measure flexibility/dynamics**

# Beyond Primary Structure: The Peptide Bond



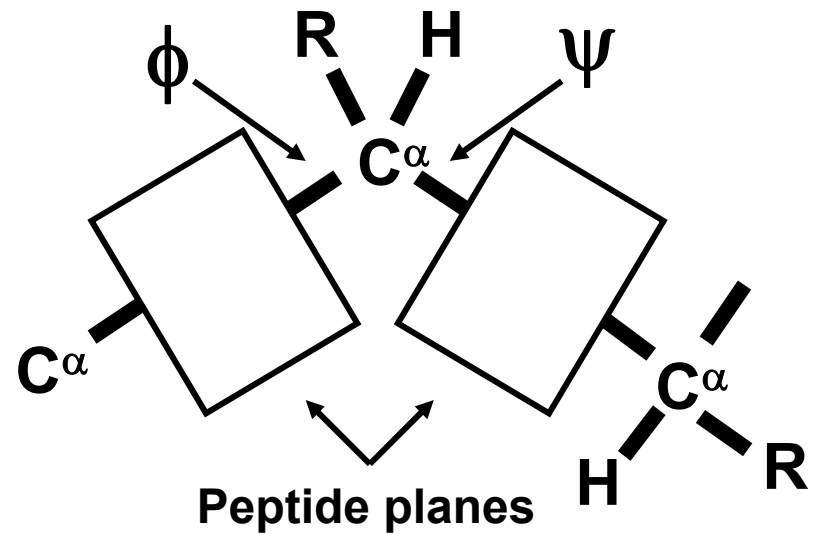
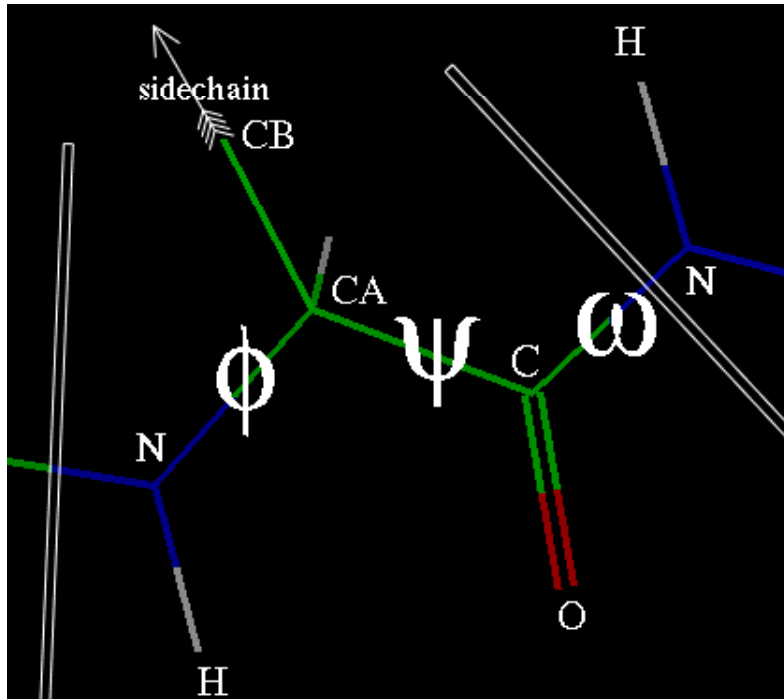
➤ Peptide plane is flat  
 $\omega$  angle  $\sim 180^\circ$

➤ Partial double-bond:



Resonance structures

# Implications of Peptide Planes



- $\omega$  angle varies little,  $\phi$  and  $\psi$  angles vary a lot
- Many  $\phi/\psi$  combinations cause atoms to collide
- Each residue is sandwiched between two planes

# Secondary Structure

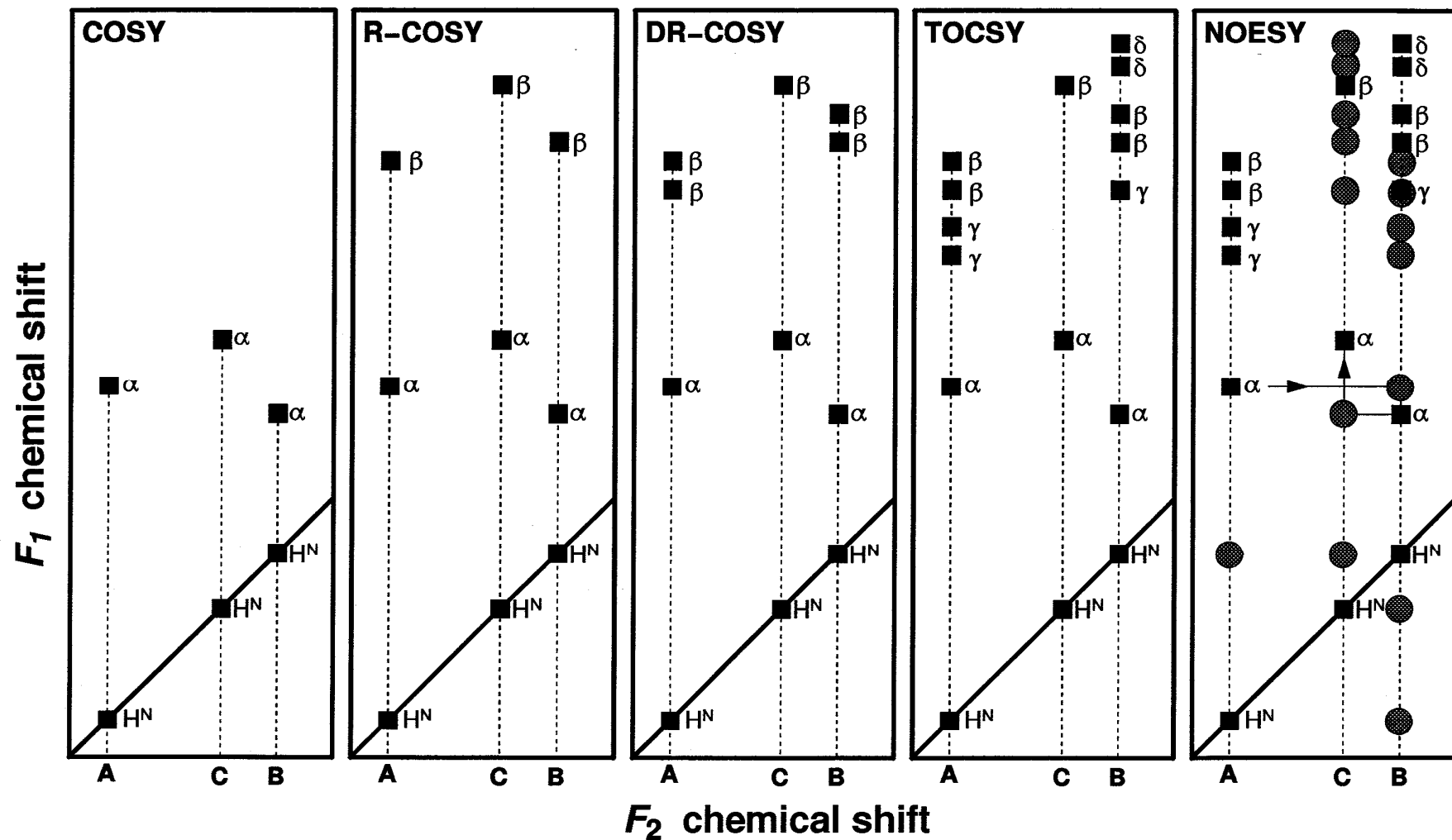
## *Local Conformation of Consecutive Residues*

- Three low energy backbone  $\phi/\psi$  combinations
  1. Right-hand helix:  $\alpha$ -,  $3_{10}$ helix ( $-40^\circ$ ,  $-60^\circ$ )
  2. Extended: antiparallel  $\beta$ -sheet ( $140^\circ$ ,  $-140^\circ$ )
  3. Left-hand helix (*rare*):  $\alpha$ -helix ( $45^\circ$ ,  $45^\circ$ )  
Glycine is special- it has no side chain!

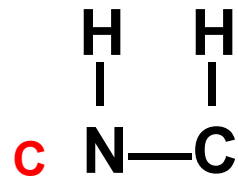
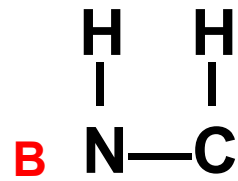
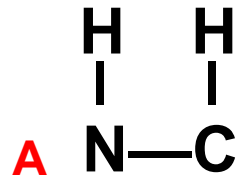
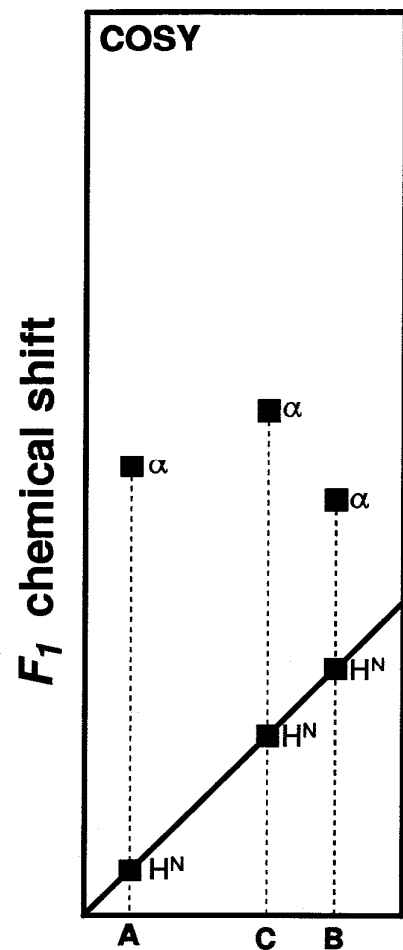
Secondary structure is readily extracted from chemical shift assignments (Chemical Shift Index- CSI):  $\psi, \phi$  calculation by Talos Software

- **Hydrogen bonds** between backbone atoms provides stability to secondary structures, NMR allows direct measurement of these bonds

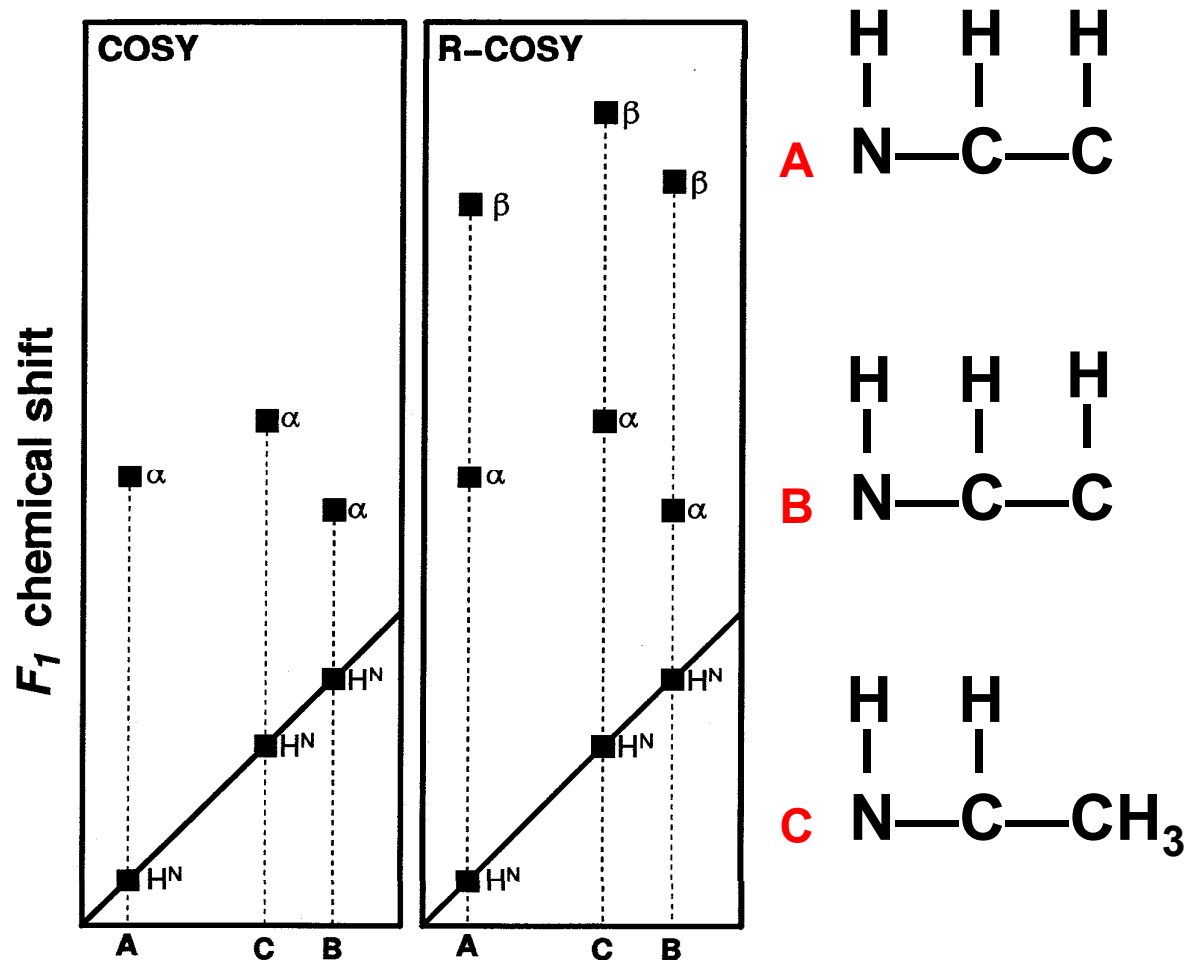
# Step 1: Identify Spin System



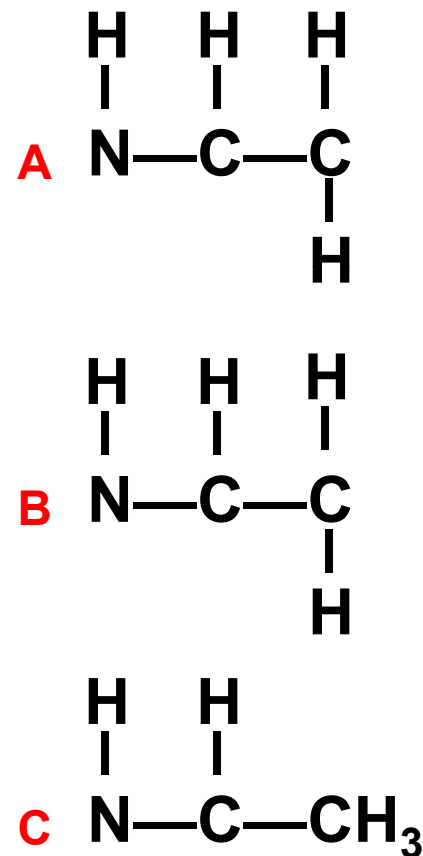
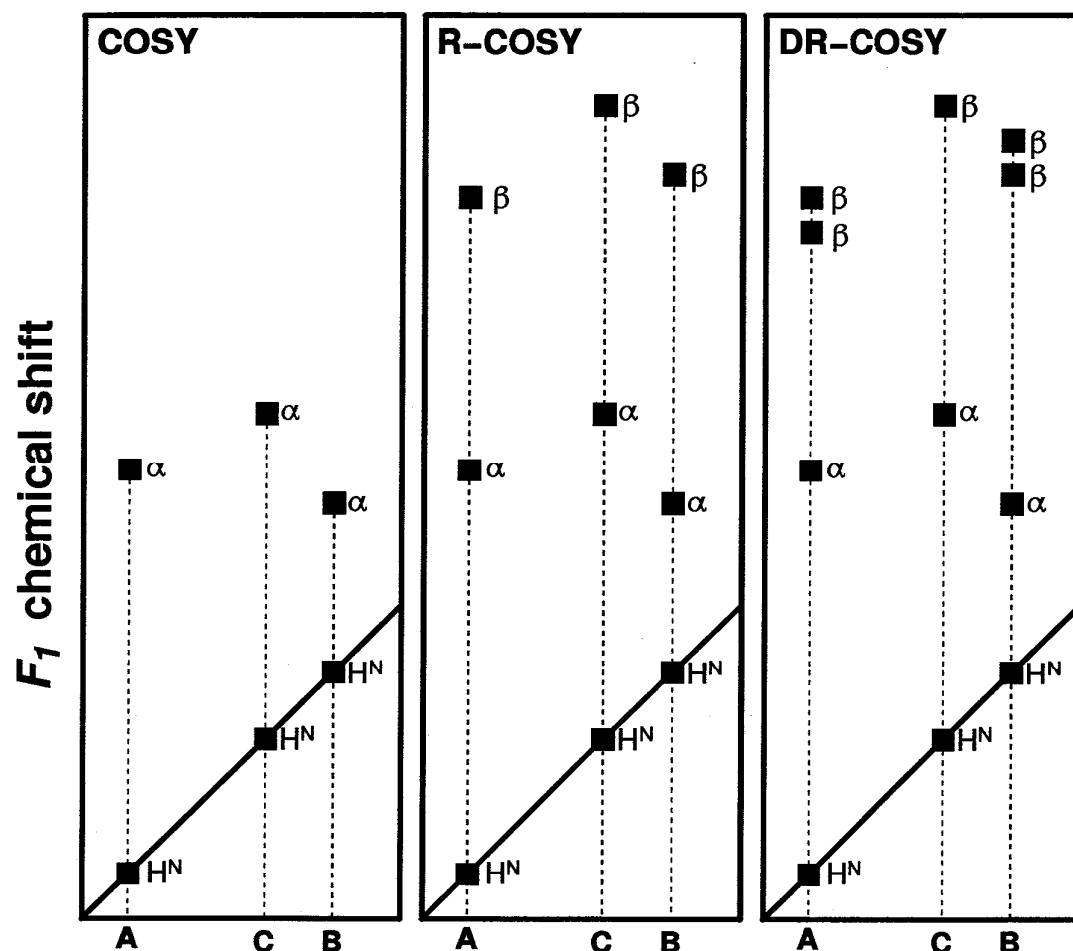
# COSY: One coupling



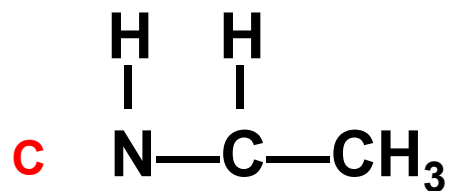
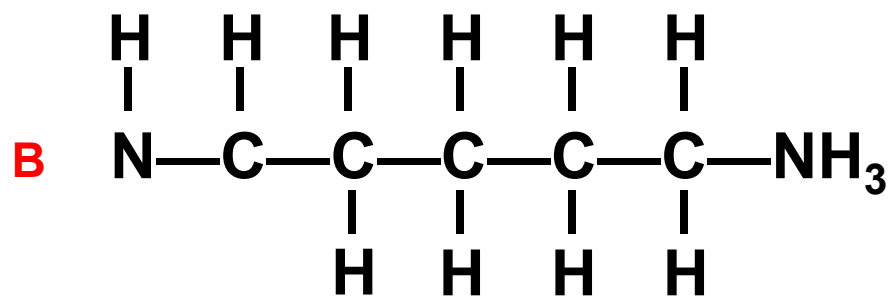
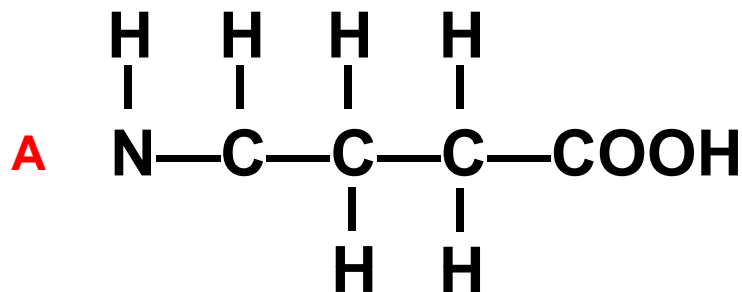
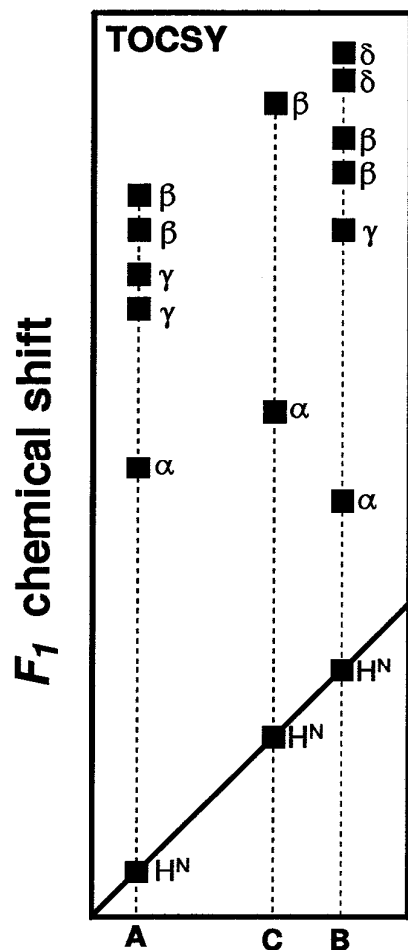
# R-COSY: Add A 2nd Coupling



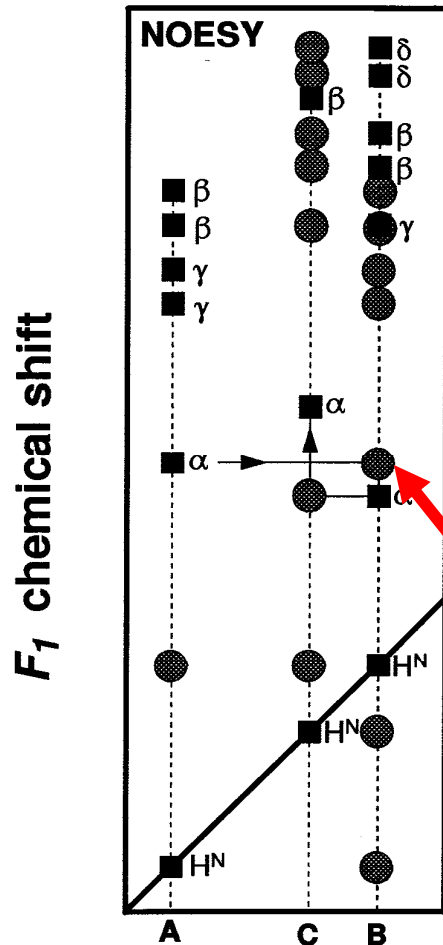
# DR-COSY: Add A 3rd Coupling



# TOCSY: All Coupled Spins



# Step 2: Fit Residues in Sequence



**A - B - C**

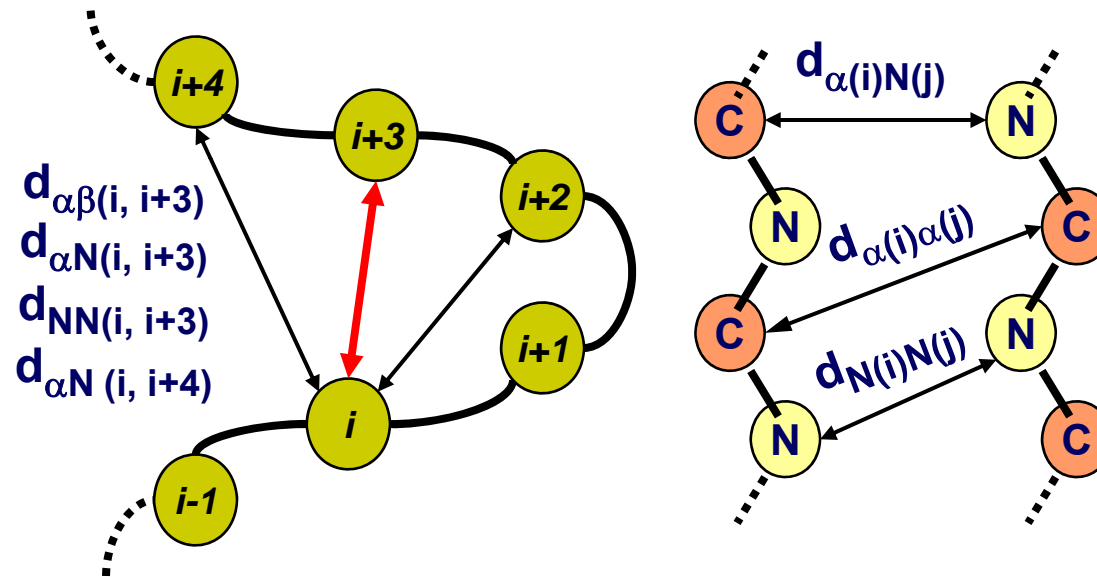
## Peaks in NOESY spectra

- Same as scalar coupling peaks
- Peaks from residue i to i+1

**A → B (B → C)**

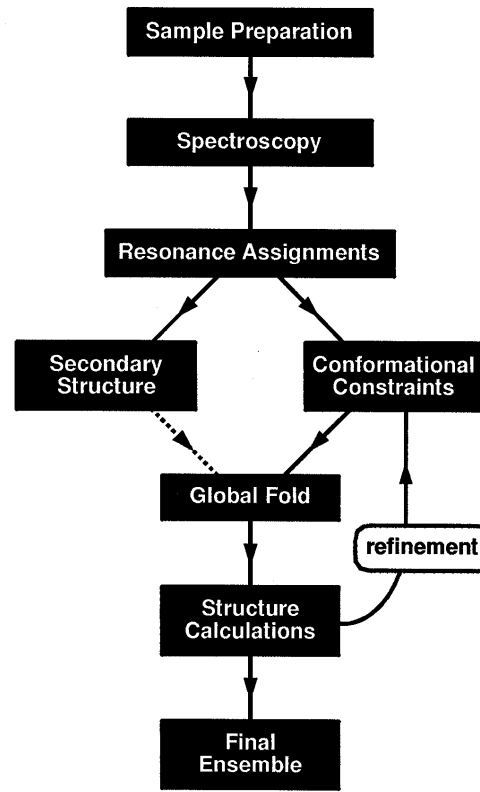
Strong NOE 1.8 - 2.7 Å  
Medium NOE 1.8 - 3.3 Å  
Weak NOE 1.8 - 5.0 Å

# Distance Restraints for helix and sheet

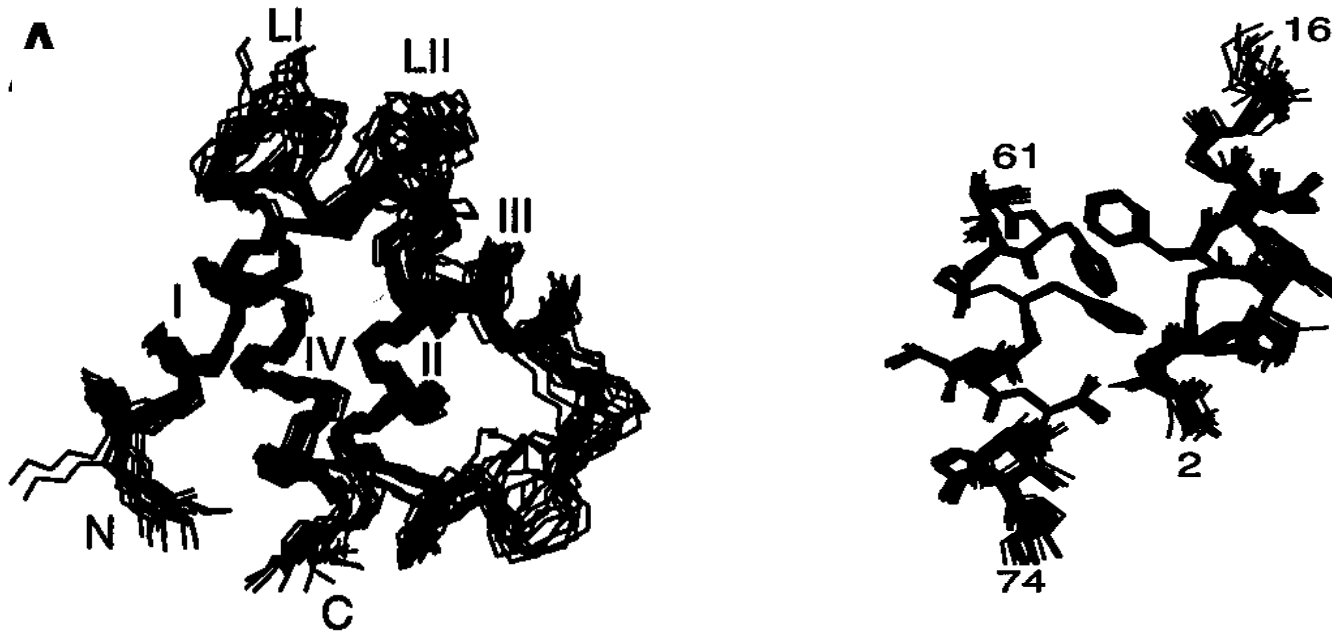


# NMR Structure Calculations

- Objective is to determine all conformations consistent with the experimental data
- Programs are available that perform automated assignment.
- NMR data are often not perfect: noise, incomplete data → multiple solutions (conformational ensemble)

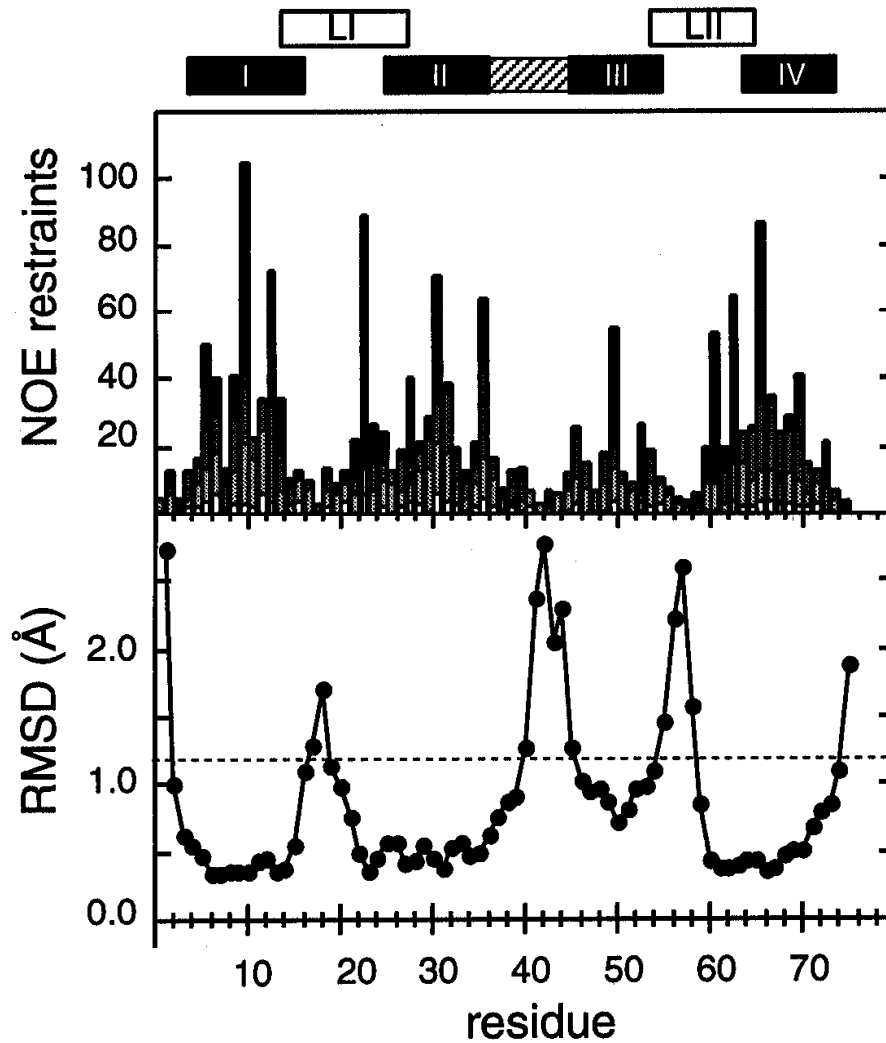


# Assessing the **A**ccuracy and **P**recision Variable Resolution Structures are reported



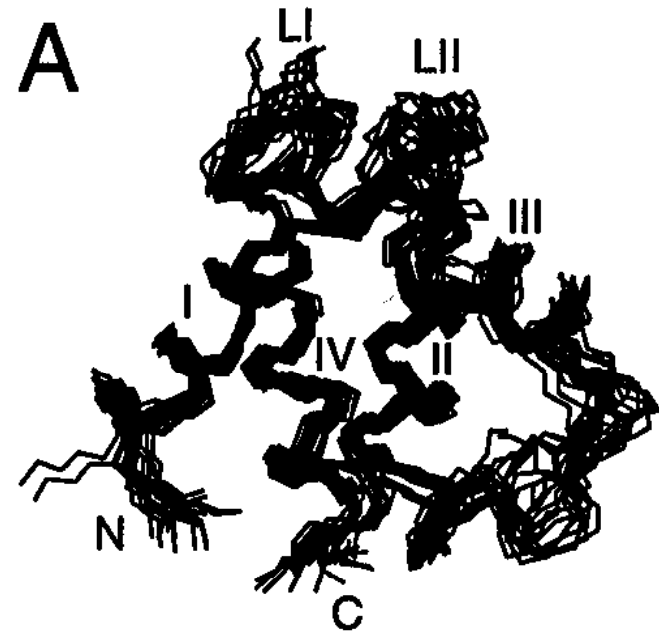
- Number of experimental restraints (A/P)
- Violation of constraints- number, magnitude (A)
- Compare model and exptl. parameters (A)
- Comparison to known structures: PROCHECK (A)
- Molecular energies (A)
- RMSD of structural ensemble (P)

# Restraints and Uncertainty



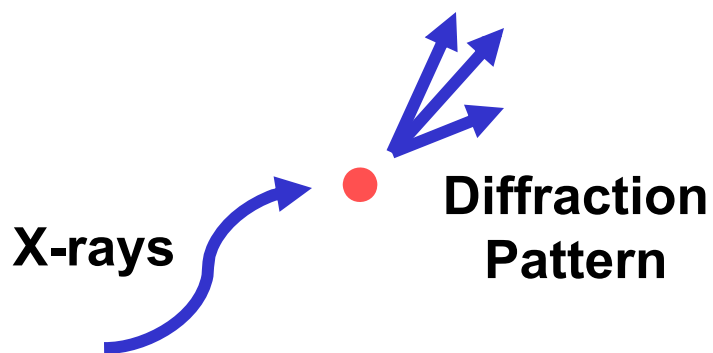
➤ Large # of restraints = low values of RMSD

➤ The most important restraints are long-range



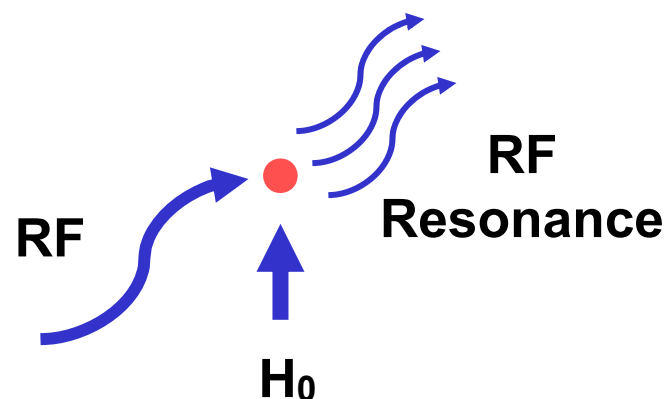
# Accuracy/Precision Determined Differently for X- ray and NMR

X-ray



- Direct detection of atom positions
- Crystals

NMR



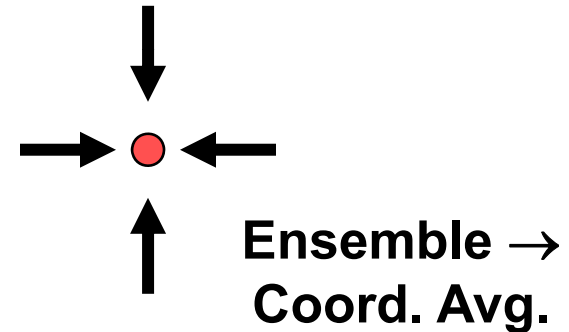
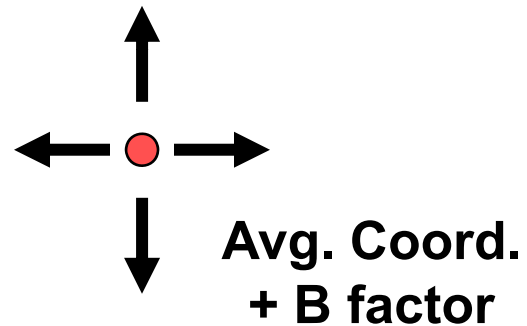
- Indirect detection of H-H distances
- In solution

# Variability: Uncertainty and Flexibility in Experimental Structures

X-ray

NMR

## •Uncertainty

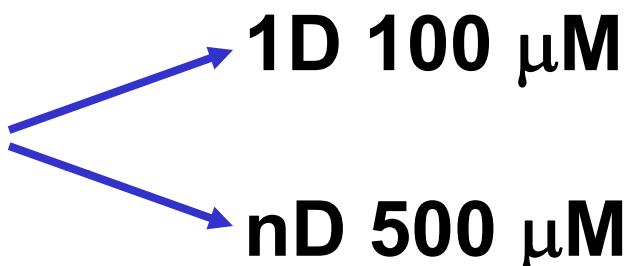


## •Flexibility

Mix static + dynamic

Measure motions

# Practical Issues: Sample Preparation

- **Concentration:** 

1D 100 $\mu\text{M}$	50 $\mu\text{M}$
	<b>Cryoprobe</b>
nD 500 $\mu\text{M}$	250 $\mu\text{M}$
- **Volume:** 500  $\mu\text{L}$ , 200  $\mu\text{L}$
- **Quantity:** @ 20kDa  $\rightarrow$  100  $\mu\text{M}$  = 1 mg
- **Purity** > 95%, buffers
- **Sensitivity** ( $\gamma$ )  $\rightarrow$  isotope enrichment ( $^{15}\text{N}$ ,  $^{13}\text{C}$ )

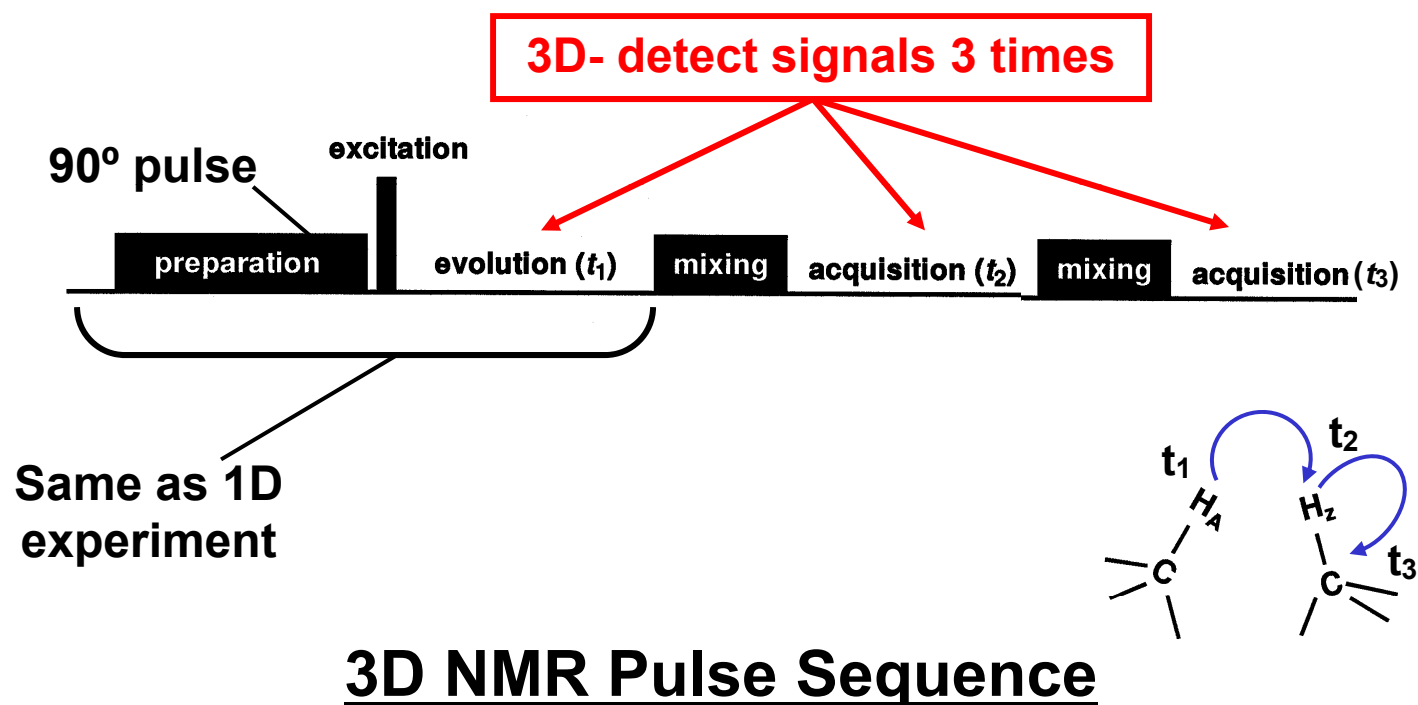
# Practical Issues: Molecular Weight

**\*Symmetry reduces complexity\***

**8 x 10 kDa  $\neq$  80 kDa**

- **30-40 kDa for 3D structure  $\rightarrow$  domains**
- **40-100 kDa: residue-, site-, and atom-specific labeling, **uniform deuteration****
- **TROSY (Transverse Relaxation Optimized [NMR] Spectroscopy)**

# Multi-Dimensional NMR: Built on the 2D Principle



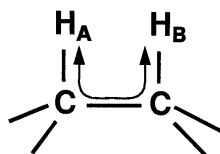
- *Experiments are composites*; Increase dimensionality of spectra to better resolve signals: 1 → 2 → 3 → 4

# Acronyms For Basic Experiments *Differ Only By The Nature Of Mixing*

Homonuclear

Heteronuclear

Scalar Coupling



COSY

HSQC

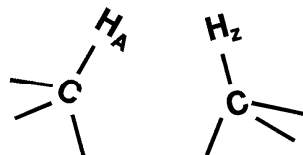
TOCSY

Hetero-TOCSY

Multiple  
Quantum

HMQC

Dipolar Coupling



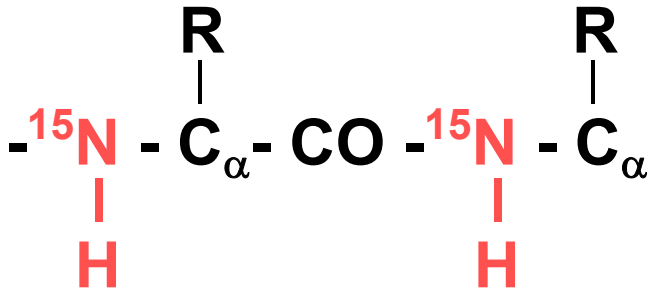
NOESY

NOESY-HSQC

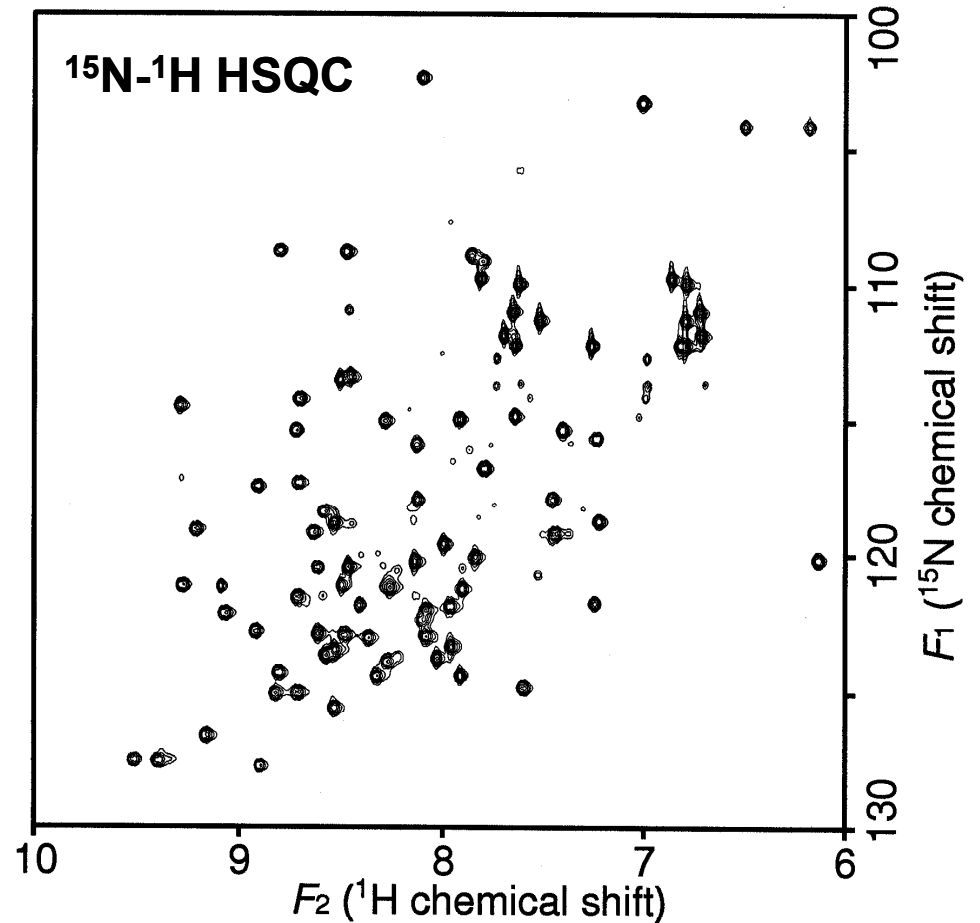
NOESY-HMQC

# Double-Resonance Experiments

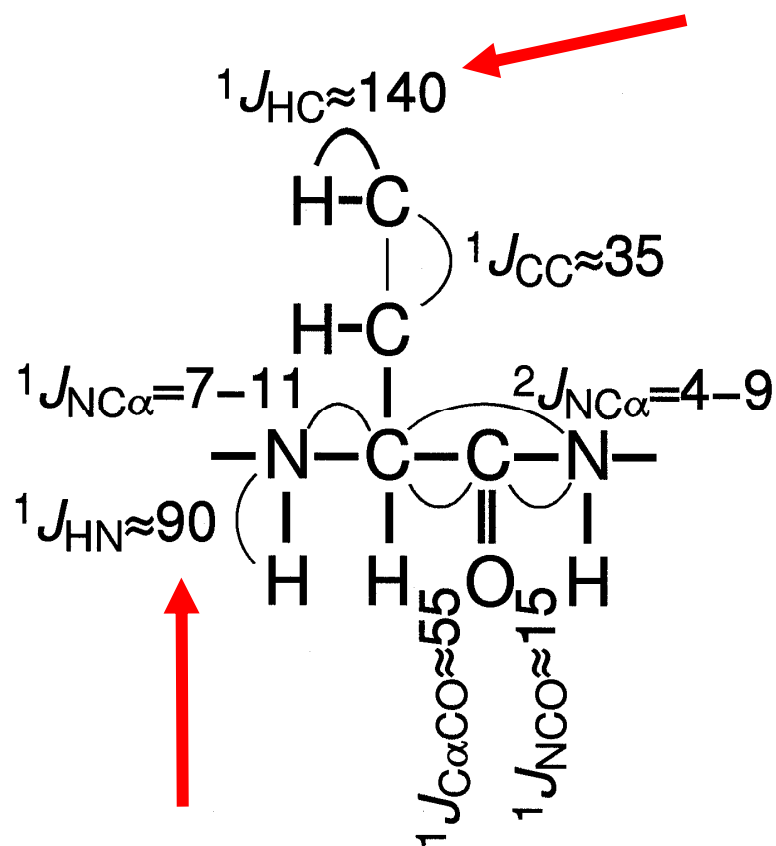
*Increases Resolution/Information Content*



- Detect signals from heteronuclei ( $^{13}\text{C}$  or  $^{15}\text{N}$ )
- Better resolution of signals/chemical shifts  
not correlated between nuclei
- More information to identify signals
- Lower sensitivity to MW of protein

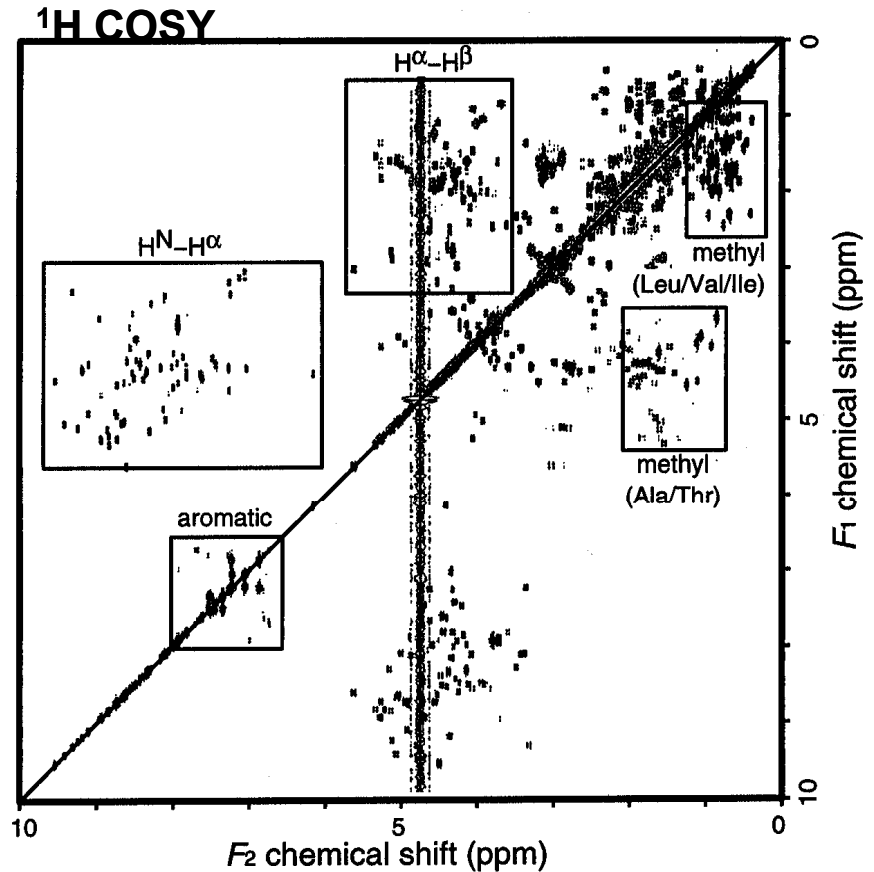
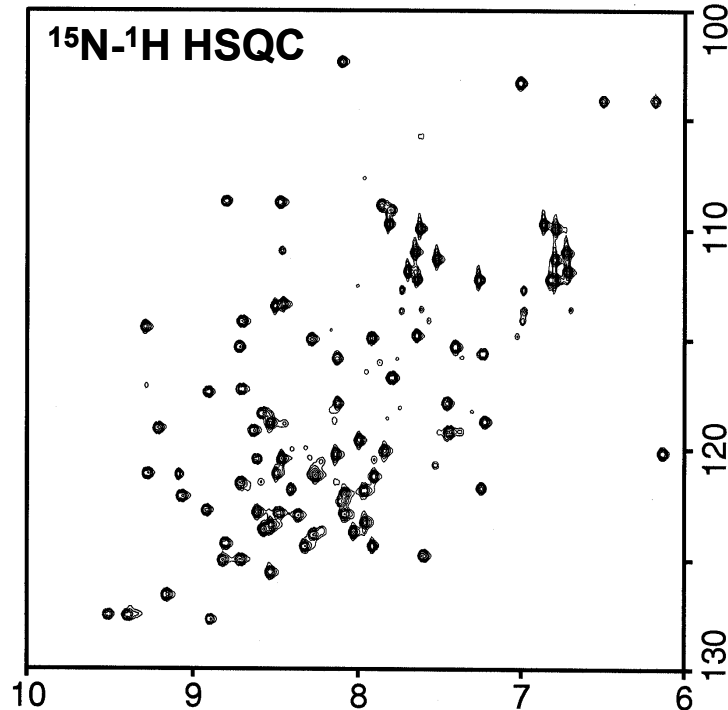


# Large Scalar Couplings → Less Sensitive to MW of the Protein

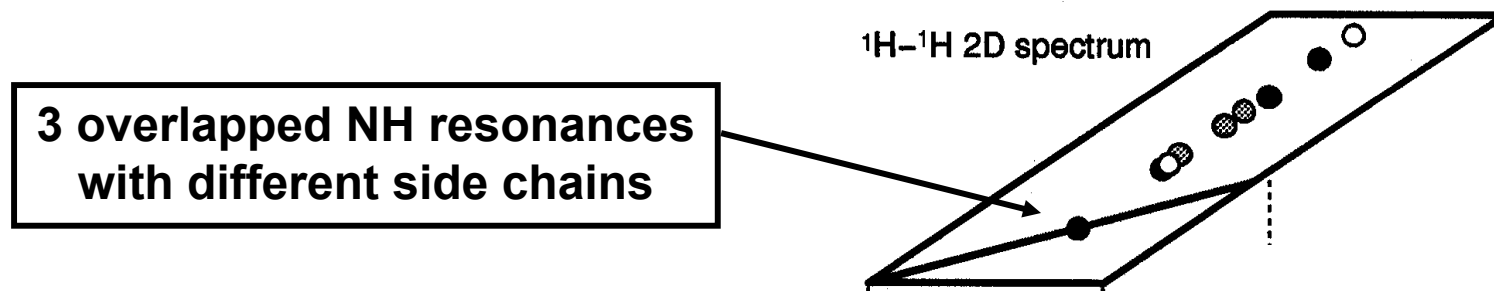


- Superior to  $^1H$  homonuclear NMR: all  $J_{H-H} < 20$  Hz
- Mixing is faster so less time for signal to relax

# Protein Folding and Fingerprints

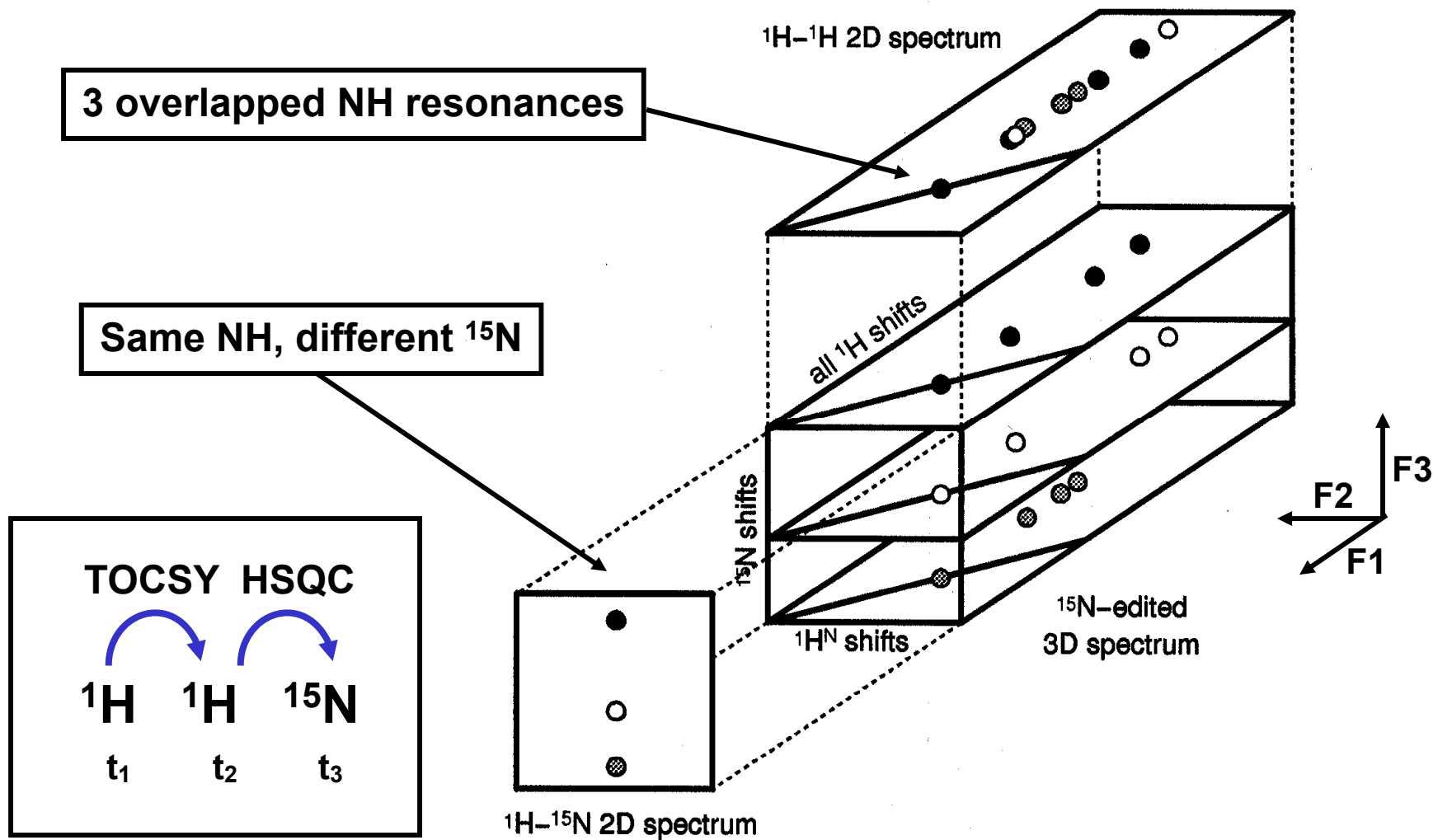


# $^{15}\text{N}$ Dispersed $^1\text{H}$ - $^1\text{H}$ TOCSY



Add a 3rd dimension separating out  $\text{H}^{\text{N}}$  overlaps by their  $^{15}\text{N}$  frequency

# $^{15}\text{N}$ Dispersed $^1\text{H}$ - $^1\text{H}$ TOCSY



# Heteronuclear ( $^1\text{H}$ , $^{13}\text{C}$ , $^{15}\text{N}$ ) Strategy

- One bond at a time - all atoms (except O)
- Even handles backbone  $^{15}\text{N}^1\text{H}$  overlaps  
→ disperse with backbone



- Het. 3D/4D increases signal resolution

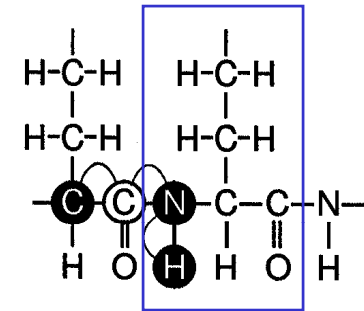
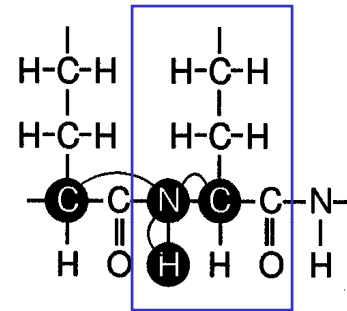


- Works on bigger proteins because one bond scalar couplings are larger

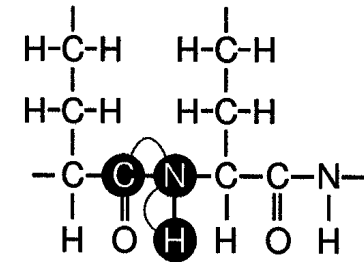
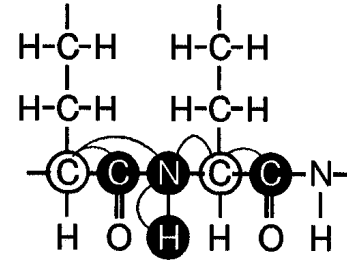
# Heteronuclear Assignments: Backbone Experiments

Names of scalar experiments based on atoms detected

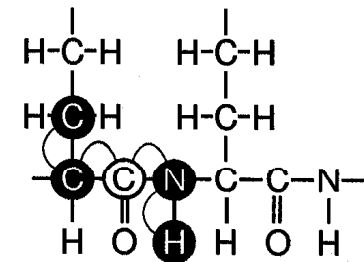
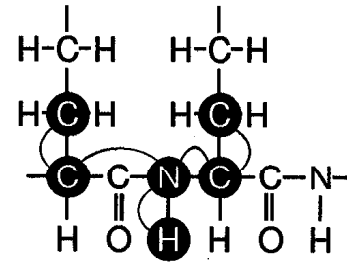
HNCA / HN(CO)CA



HN(GA)CO / HNCO



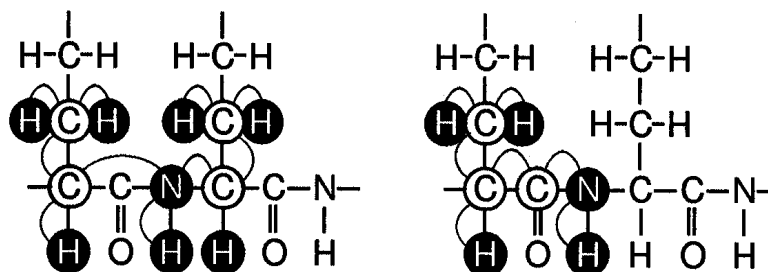
HNCACB / HN(CO)CACB



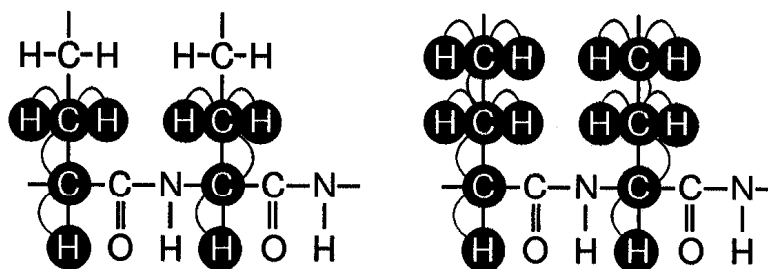
*Direct assignment of Consecutive residues  
(without NOESY)*

# Heteronuclear Assignments: Side Chain Experiments

HBHA(CBCA)NH /  
HBHA(CBCACO)NH



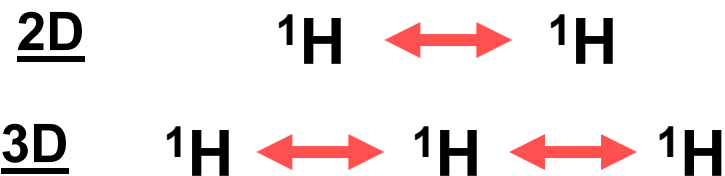
HCCH-COSY /  
HCCH-TOCSY



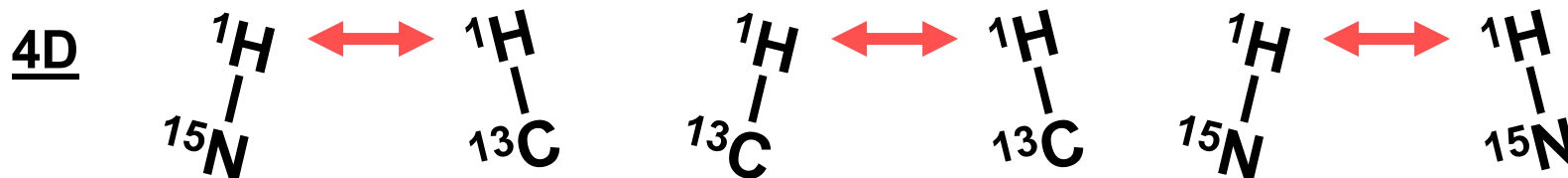
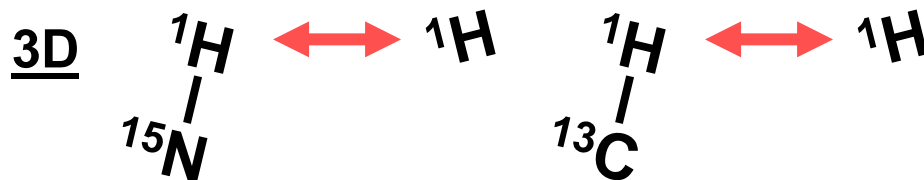
**Multiple redundancies increase reliability**

# Approaches to Identifying NOEs

- $^1\text{H}$ - $^1\text{H}$  NOESY

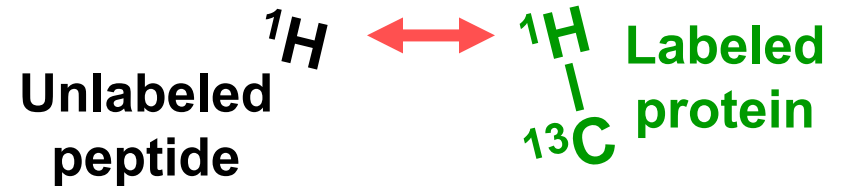


- $^{15}\text{N}$ - or  $^{13}\text{C}$ -dispersed  $^1\text{H}$ - $^1\text{H}$  NOESY



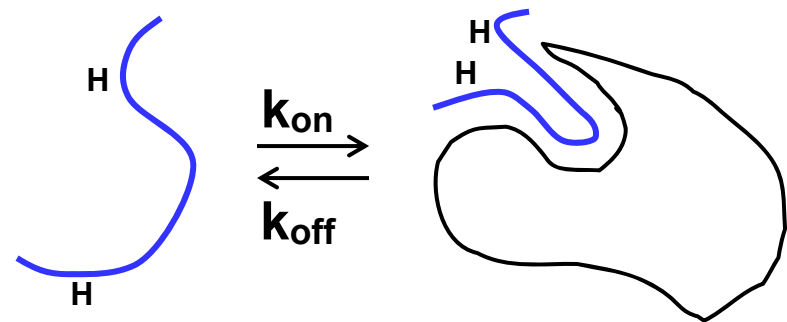
# Special NOESY Experiments

- **Filtered, edited NOE:** *based on selection of NOEs from two molecules with unique labeling patterns.*



**Only NOEs at the interface**

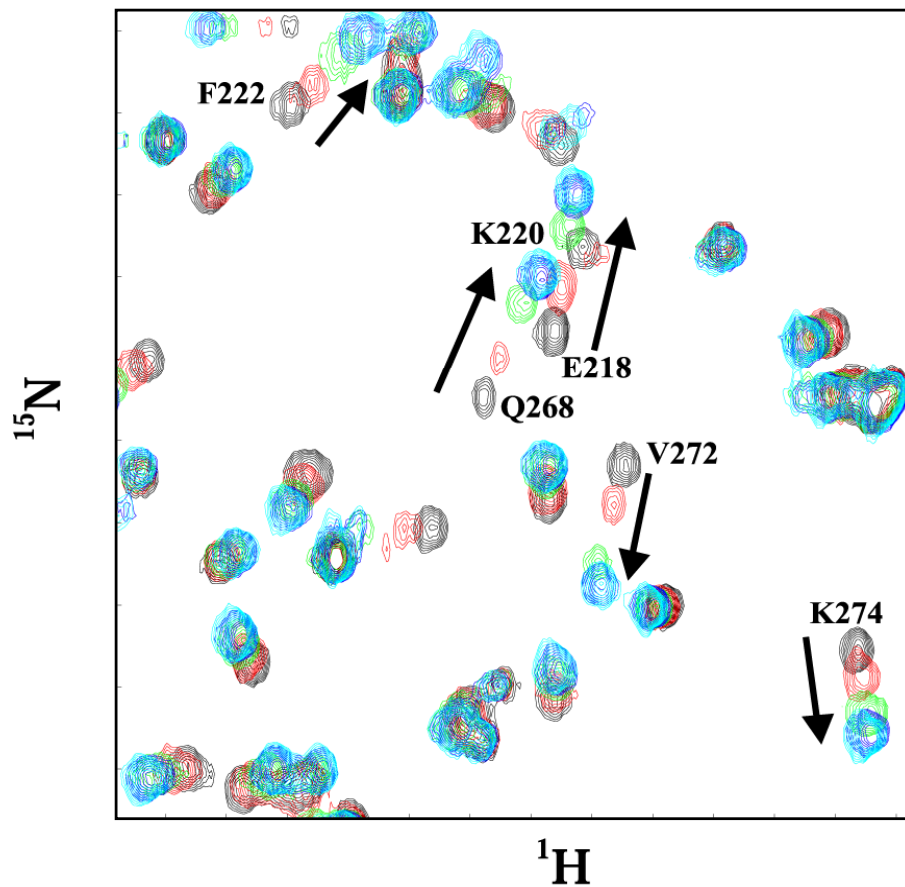
- **Transferred NOE:** *based on 1) faster build-up of NOEs in large versus small molecules; 2) Fast exchange 3) NOEs of bound state detected at resonance frequencies of free state*



**Only NOEs from bound state**

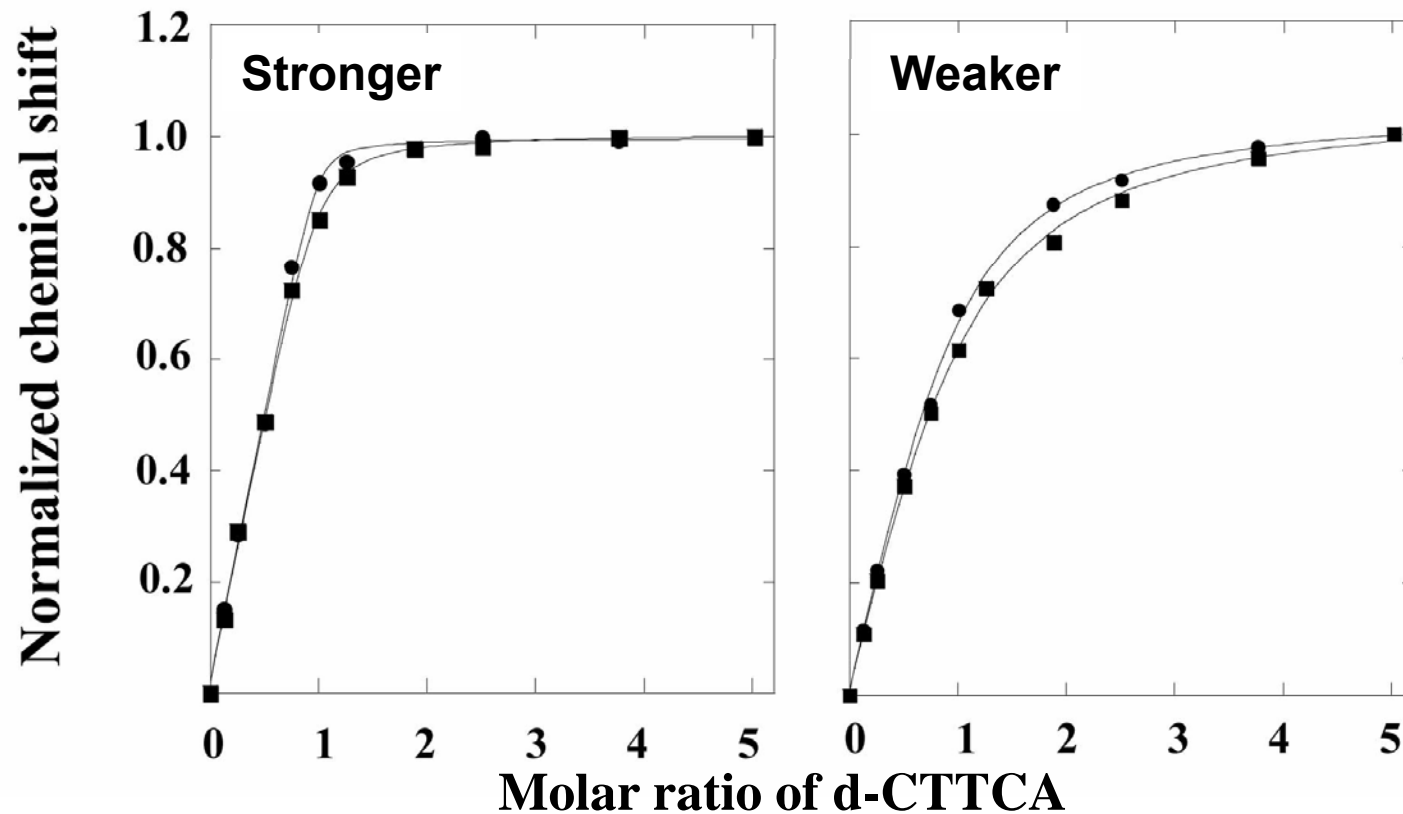
# NMR to Study Interactions

Titration monitored by  $^{15}\text{N}$ - $^1\text{H}$  HSQC



- Monitor the binding of molecules
- Determine binding constants (discrete off rates, on rates)
- Sequence and 3D structural mapping of binding interfaces

# Binding Constants From Chemical Shift Changes



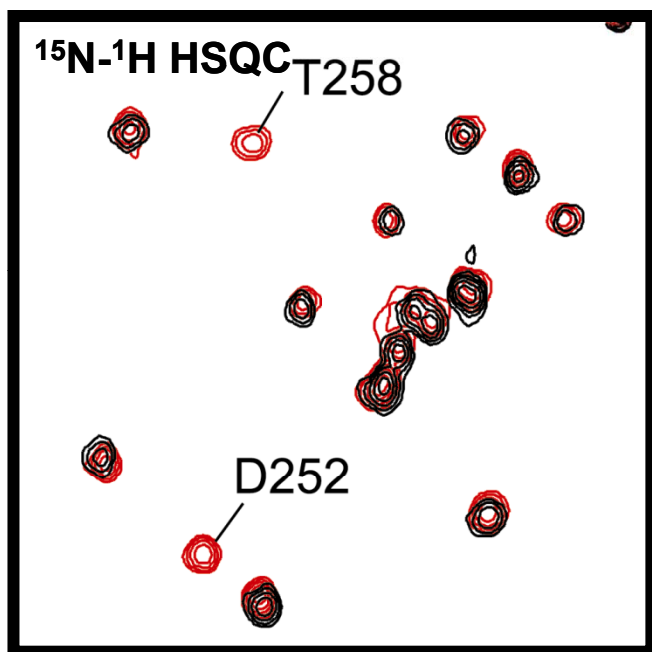
➤ *Fit change in chemical shift to binding equation*

Arunkumar et al., JBC (2003)

[http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list\\_uids=12881520](http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list_uids=12881520)

# Probe Binding Events by NMR

*$^{15}\text{N}$ -RPA32C + Unlabeled XPA<sub>1-98</sub>*



**RPA32C**

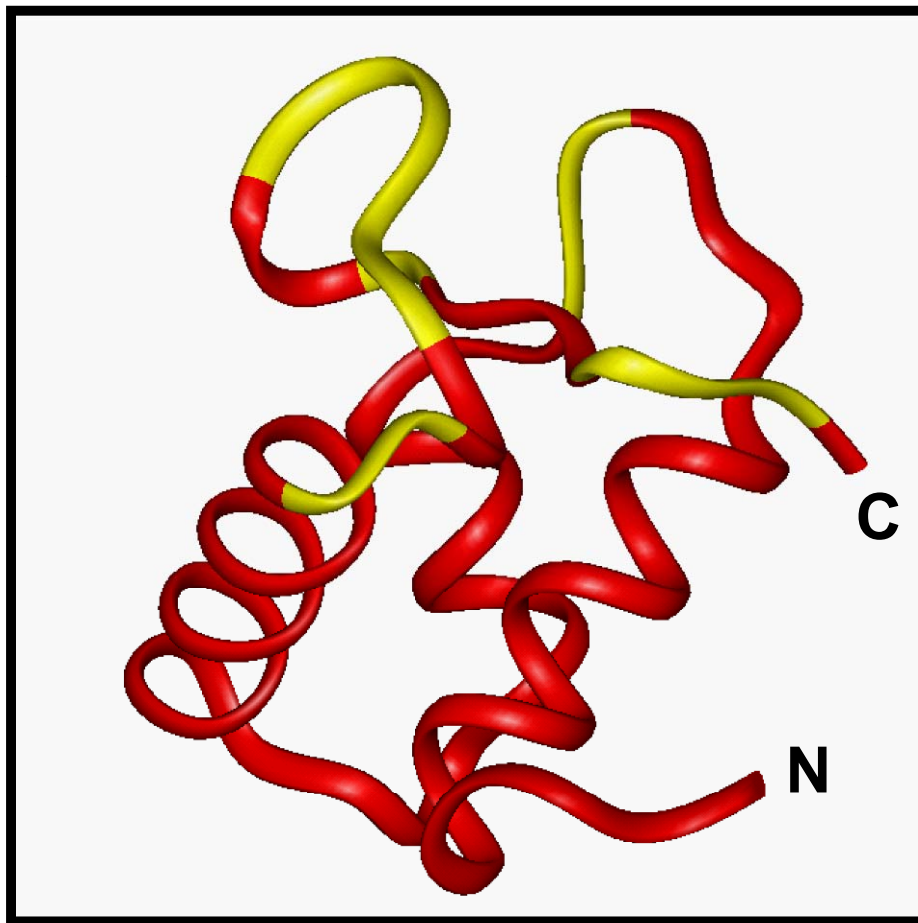
**RPA32C + XPA<sub>1-98</sub>**

- 19 residues affected
  - *Discrete binding site*
- Signal broadening → exchange between the bound and un-bound state
  - $K_d \sim 1 \mu\text{M}$

Mer et al., Cell (2000)

[http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list\\_uids=11081631](http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list_uids=11081631)

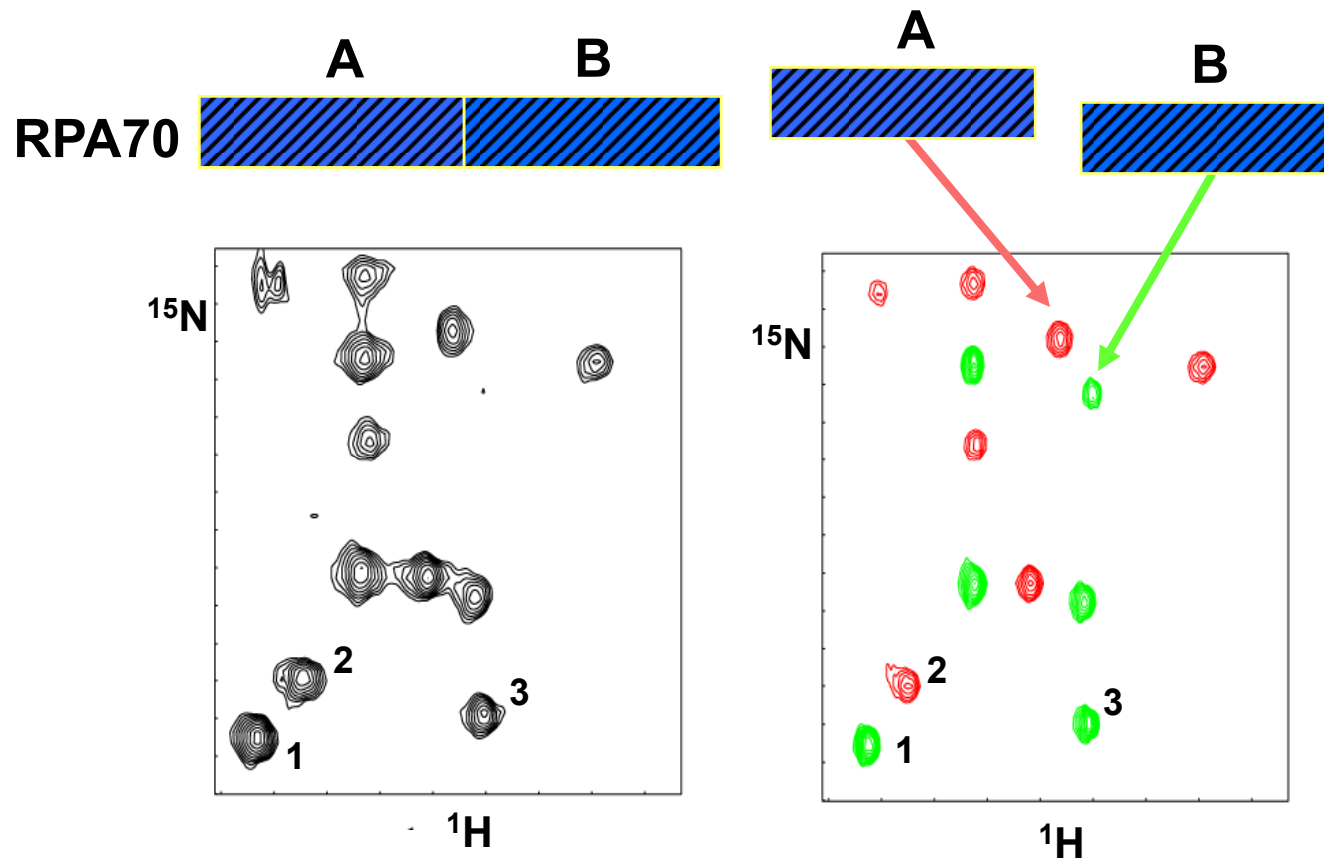
# Map XPA Binding Site on RPA32C Using NMR



- Map chemical shift perturbations on the structure of RPA32C
- Can even map directly on to sequence with no structure

# Folding and Domain Structure

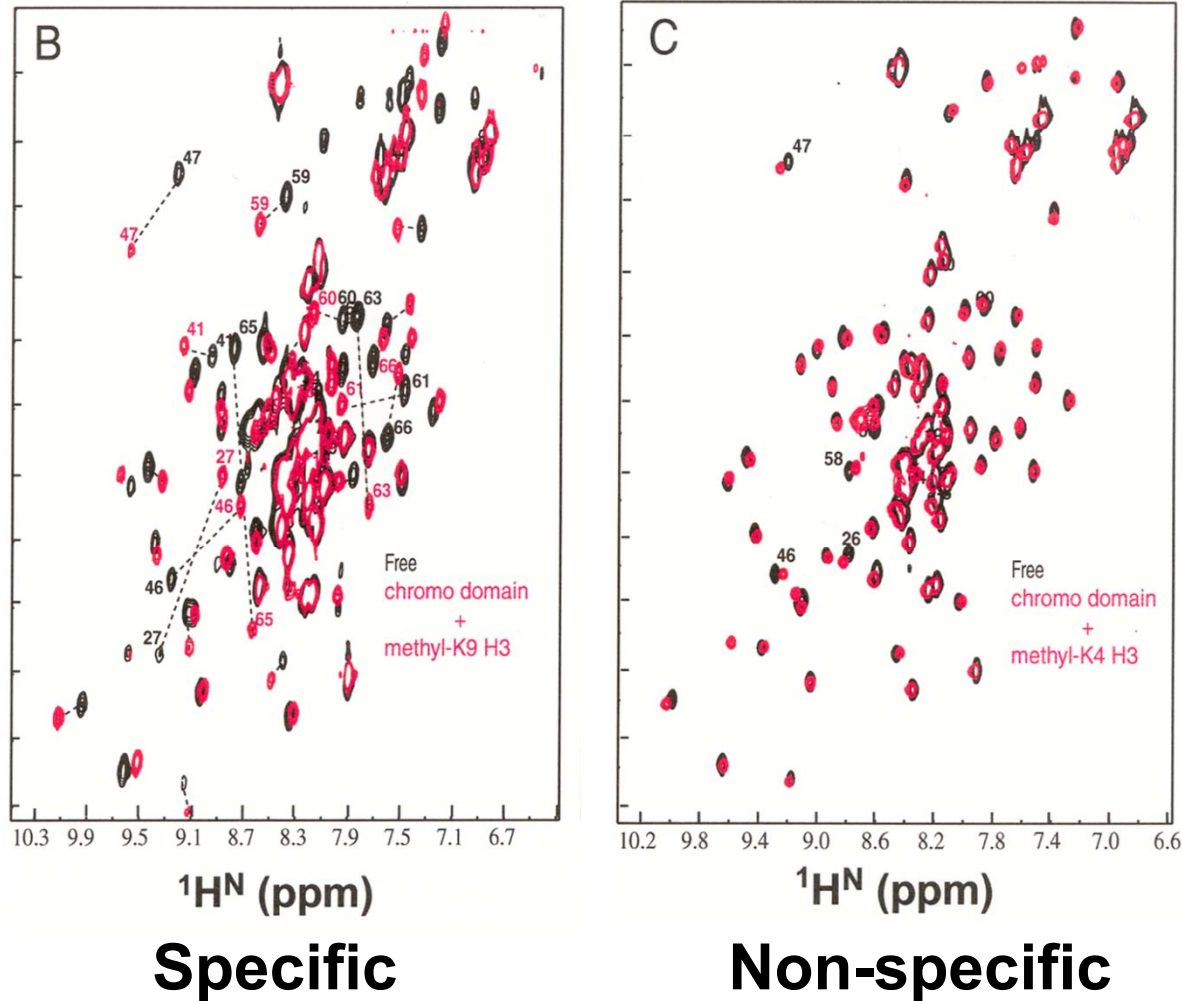
*Are domains packed together or independent?*



**Chemical shift is extremely sensitive**

- If peaks are the same, structure is the same
- If peaks are different, the structure is different but we don't know how much

# Binding of histone H3 peptide to HP1 chromodomain requires H3K9 methylation



Jacobs et al (2001) EMBO J.

[http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list\\_uids=11566886](http://www.ncbi.nlm.nih.gov/entrez/query.fcgi?cmd=Retrieve&db=PubMed&dopt=Citation&list_uids=11566886)