

Lecture 4 Block Model

Last time, introduced transfer functions
input impedance
output impedance

transfer functions: $V_{out} = G V_{in}$

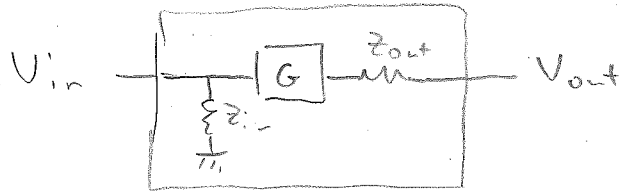
input impedance $V_{in} \xrightarrow{z_{in}}$



output impedance $V_{eff} \xrightarrow{z_{out}} V_{out}$

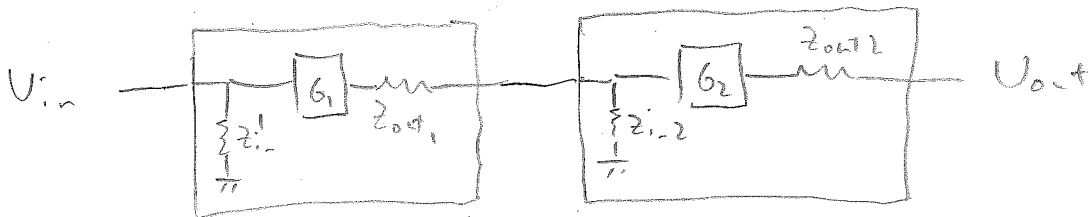


Put together in "block model" for circuit:



Elements in box give effective description of circuit. "Black box" approach: avoid worrying about details of how circuit works.

Mostly useful when combining circuits:



Can see that if $|z_{out,1}| \ll |z_{in,2}|$, have $V_{out} = G_2 G_1 V_{in}$

Transfer functions just multiply.

If $|z_{out,1}| \approx |z_{in,2}|$, form voltage divider, can calculate effect.

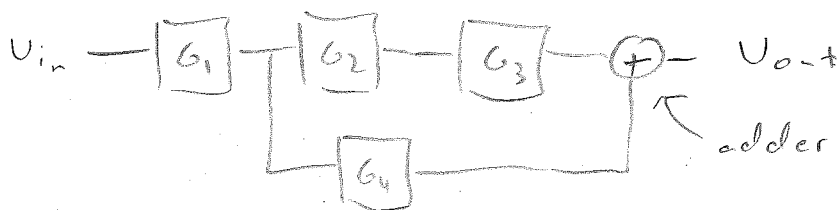
Warning: input impedance does, in general,
depend on output load
output impedance depends in general
on input current

So block model really only works well
when $|Z_{out}| \ll |Z_{in}|$

\Rightarrow try to design circuit blocks with low Z_{out} ,
high Z_{in}

We'll see tools to achieve this.

When we do, just analyze circuit as blocks:



$$V_{out} = G_1(G_2G_3 + G_4)V_{in}$$

Very powerful approach.

Bode plots especially useful here:

$$G = |G| e^{i\phi} \quad g(\text{dB}) = 20 \log |G|$$

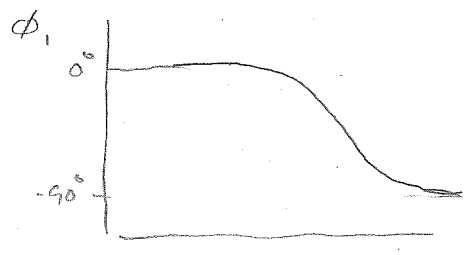
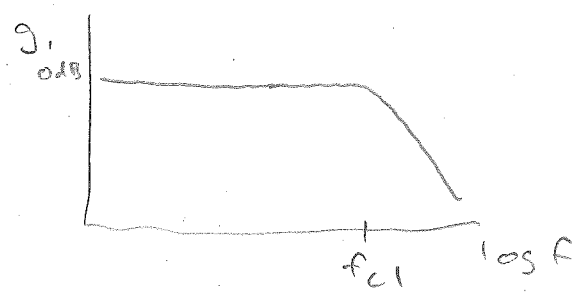
$$\begin{aligned} \text{So if } G_{TOT} &= G_1 G_2 \\ &= |G_1| |G_2| e^{i(\phi_1 + \phi_2)} \end{aligned}$$

$$\begin{aligned} g_{TOT} &= 20 \log (|G_1| |G_2|) \\ &= 20 \log |G_1| + 20 \log |G_2| \\ &= g_1 + g_2 \end{aligned}$$

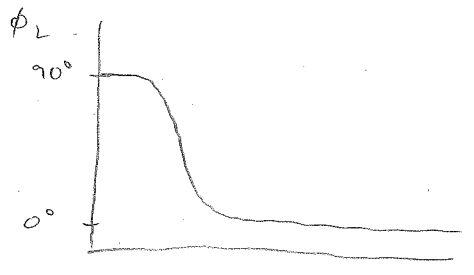
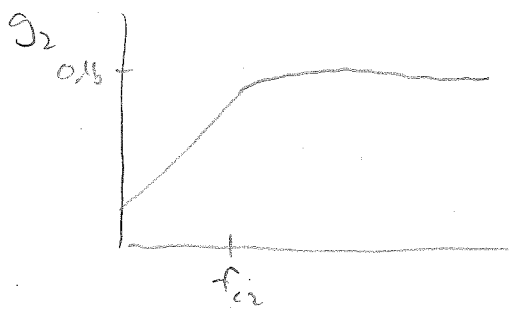
$$\text{and } \phi_{TOT} = \phi_1 + \phi_2$$

So to cascade circuits, just add Bode plot values

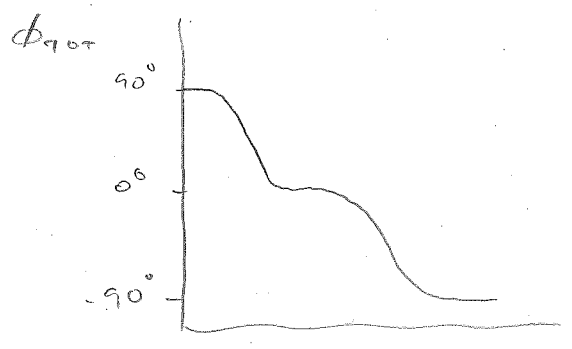
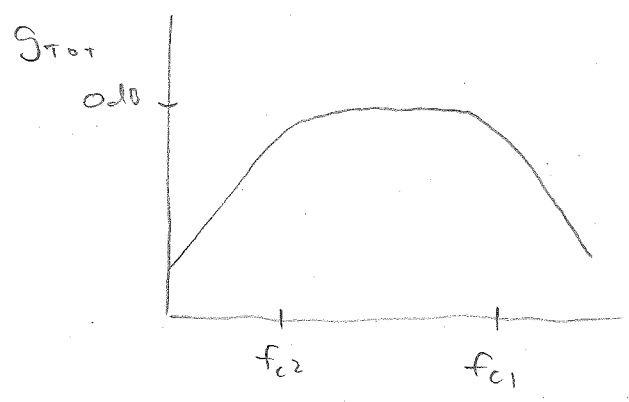
Example: Circuit 1 = low pass filter



Circuit 2 = high pass filter



Combined:



Can get a good idea what composite circuit does without any analysis.

A few comments about dBs:

I'll give $|G|$ (not in dB) as "x" multiplier

$$\text{Thus } 20 \text{ dB} = 10\times$$

$$40 \text{ dB} = 100\times$$

Some useful conversions:

$$|G| = 2\times \Rightarrow g = 20 \log 2 = 6.02 \text{ dB}$$

$$\text{Use } 2\times \approx 6 \text{ dB}$$

$$|G| = 3\times \Rightarrow g = 20 \log 3 = 9.5 \text{ dB}$$

$$\text{Use } 3\times \approx 10 \text{ dB} \quad (\text{though less accurate})$$

$$|G| = 1.1\times \Rightarrow g = 0.83 \text{ dB}$$

$$\text{Use } 1.1\times \approx 1 \text{ dB}$$

Memorizing these lets you do quick conversions in your head:

$$30 \text{ dB} = 20 \text{ dB} + 10 \text{ dB} = (10\times) \cdot (3\times) = 30\times$$

$$0.5\times = (2\times)^{-1} = -6 \text{ dB}$$

$$\frac{1}{\sqrt{2}} \times = (2\times)^{-1/2} = -3 \text{ dB}$$